

# Evaluations of nuclear weak rates relevant to astrophysical applications

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## ○ New shell-model Hamiltonians

SFO (p-shell), GXPF1J (fp-shell), USDB (sd-shell)

Spin modes -GT strengths, M1 moments- are well described.

→ Accurate evaluation of spin-dependent transition rates

## ○ $\nu$ -nucleus reactions

- $\nu$ - $^{12}\text{C}$ ,  $\nu$ - $^{56}\text{Fe}$ ,  $\nu$ - $^{56}\text{Ni}$  reactions with SFO and GXPF1J

- Nucleosynthesis of light elements,  $^7\text{Li}$  and  $^{11}\text{B}$ , and  $^{55}\text{Mn}$  in supernova explosions (SNe)

$\nu$  oscillations effects and  $\nu$  oscillation parameters

- $\nu$ - $^{40}\text{Ar}$  reactions with VMU (monopole-based universal interaction)

## ○ e-capture and $\beta$ -decay rates in stellar environments

- e-capture rates in pf-shell nuclei with GXPF1J

Type-Ia supernova explosions and nucleosynthesis

- e-capture and  $\beta$ -decay rates in sd-shell and pf-shell nuclei and cooling of stars by URCA processes

- $\beta$ -decay half-lives of waiting-point nuclei at  $N=126$  and r-process nucleosynthesis

# ○ New shell-model Hamiltonians and successful description of Gamow-Teller (GT) strengths

SFO (p-shell): GT in  $^{12}\text{C}$ ,  $^{14}\text{C}$

Suzuki, Fujimoto, Otsuka, PR C69, (2003)

GXPF1J (fp-shell): GT in Fe and Ni isotopes, M1 strengths

Honma, Otsuka, Mizusaki, Brown, PR C65 (2002); C69 (2004)

Suzuki, Honma et al., PR C79, (2009)

VMU (monopole-based universal interaction)

Otsuka, Suzuki, Honma, Utsuno et al., PRL 104 (2010) 012501

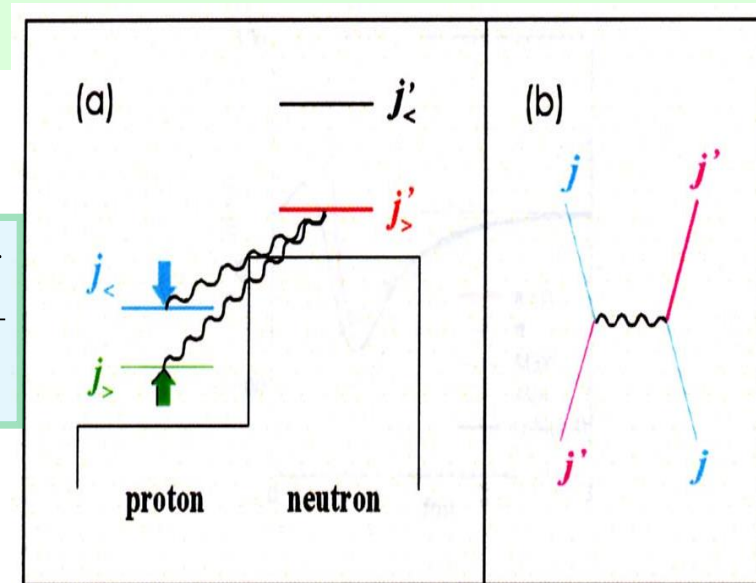
**\* important roles of tensor force**

Monopole terms of  $V_{NN}$

$$V_M^T(\mathbf{j}_1\mathbf{j}_2) = \frac{\sum_{\mathbf{J}} (2\mathbf{J} + 1) \langle \mathbf{j}_1\mathbf{j}_2; \mathbf{J}\mathbf{T} | \mathbf{V} | \mathbf{j}_1\mathbf{j}_2; \mathbf{J}\mathbf{T} \rangle}{\sum_{\mathbf{J}} (2\mathbf{J} + 1)}$$

$j_> - j_<$  : attractive

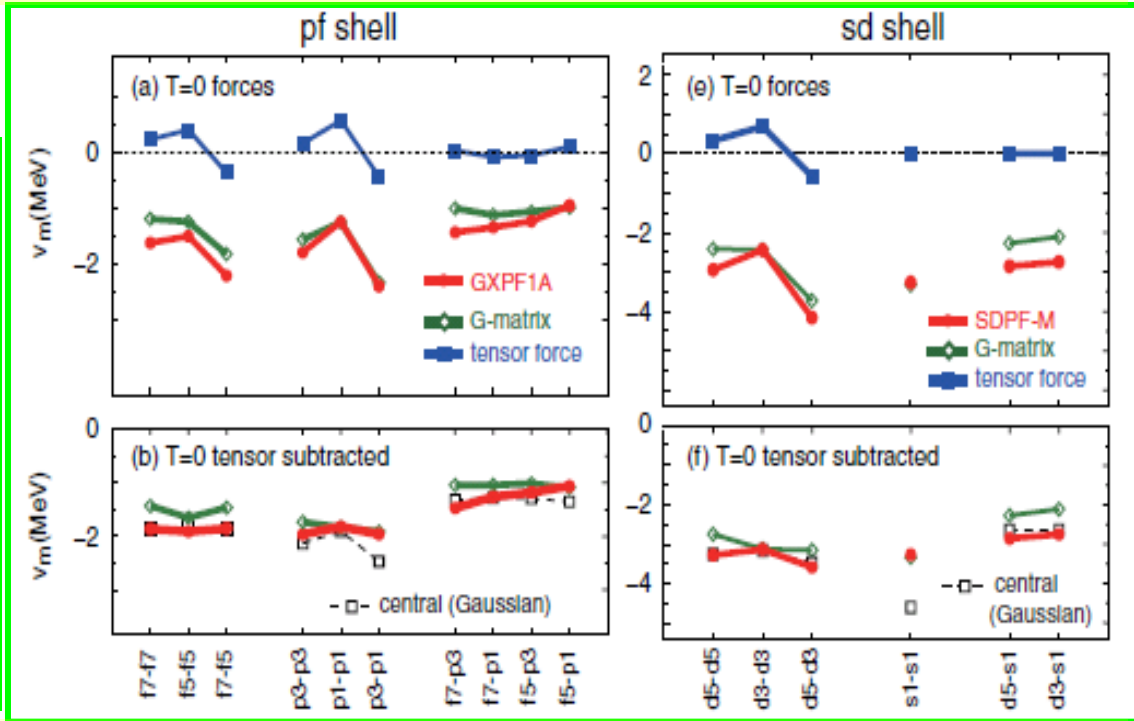
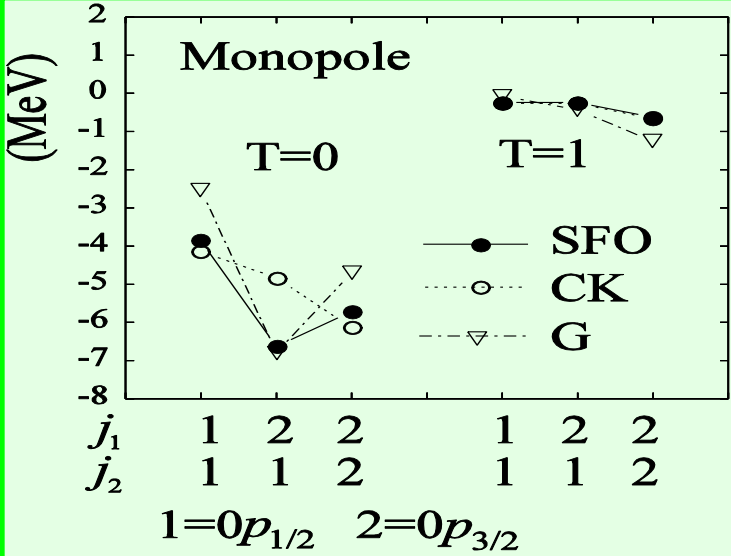
$j_> - j_>, j_< - j_<$  : repulsive



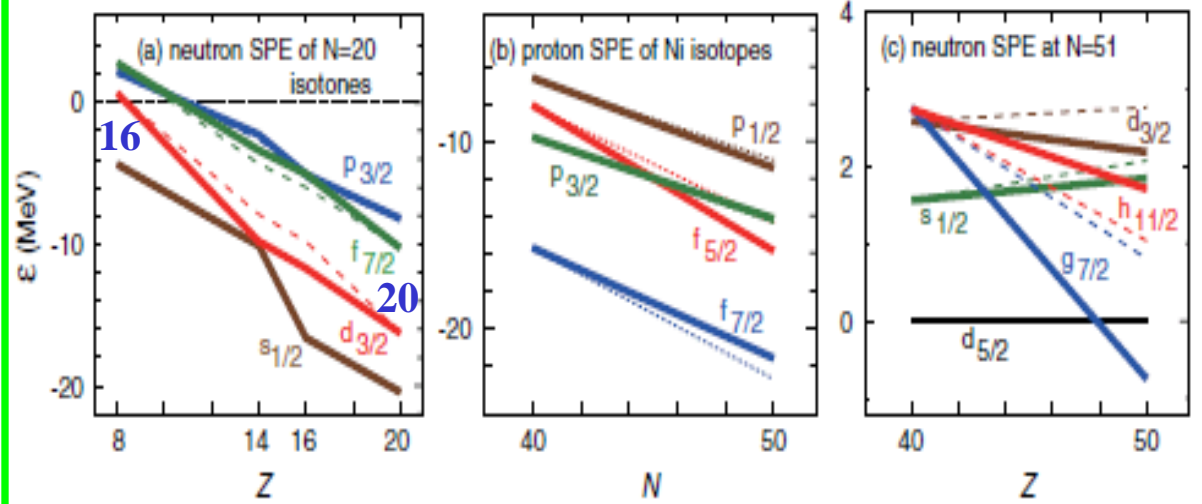
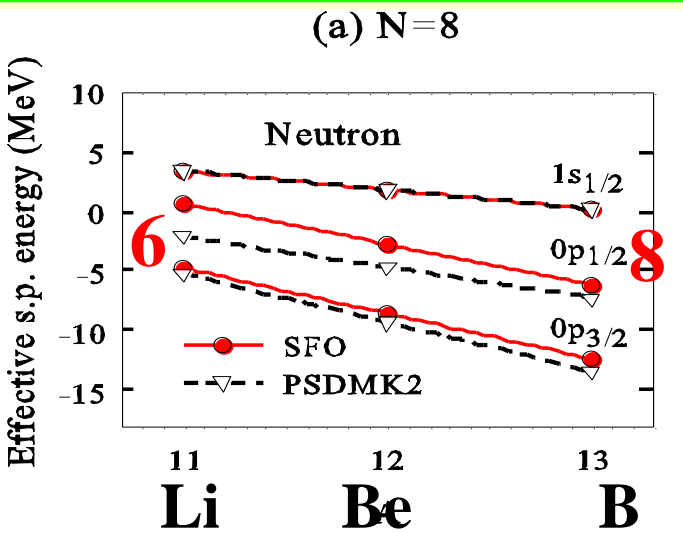
Otsuka, Suzuki, Fujimoto, Grawe, Akaishi, PRL 69 (2005)

# Monopole terms: New SM interactions vs. microscopic G matrix

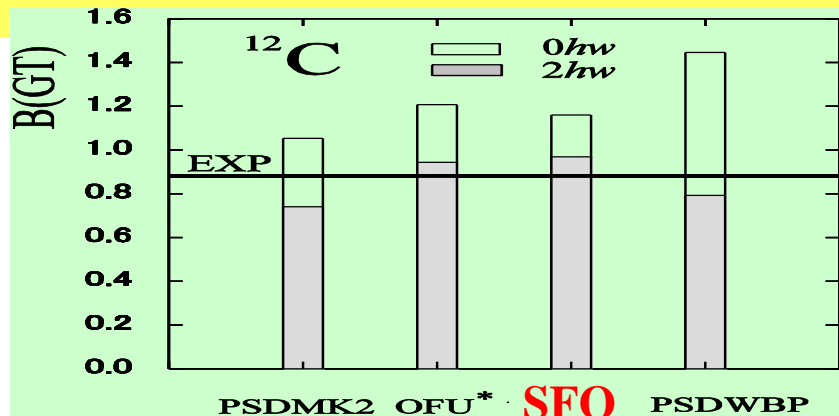
## tensor force



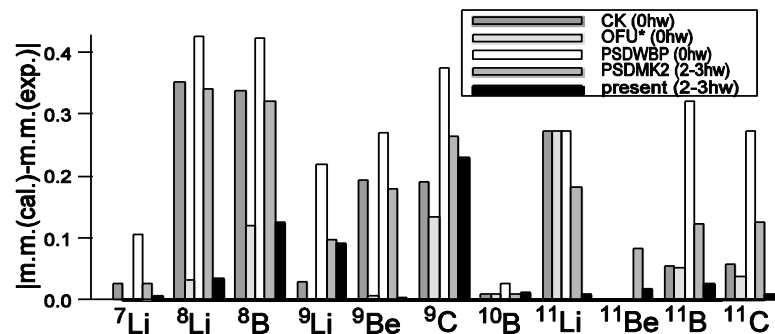
## Proper shell evolutions toward drip-lines: Change of magic numbers



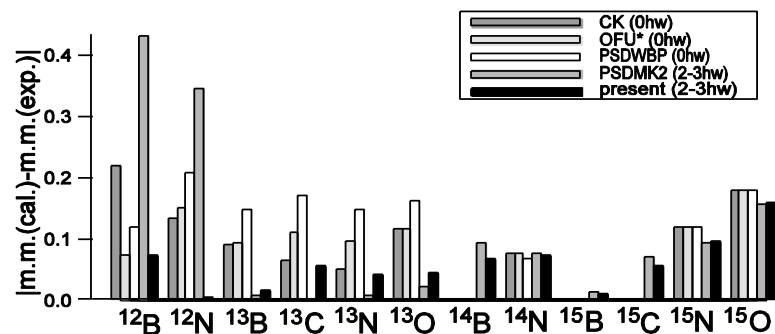
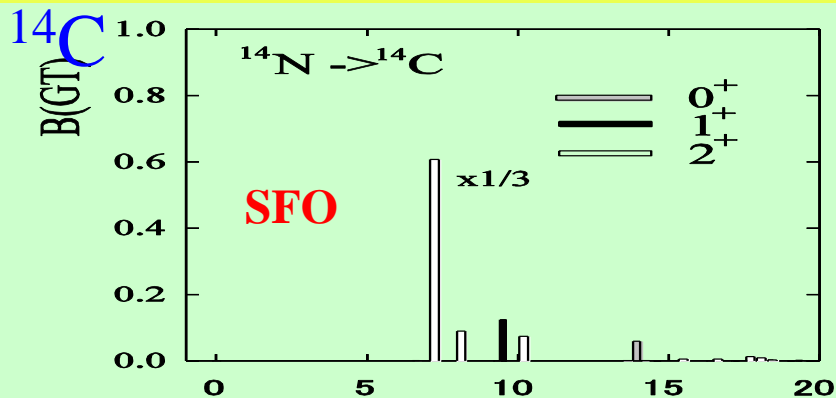
# B(GT) values for $^{12}\text{C} \rightarrow ^{12}\text{N}$



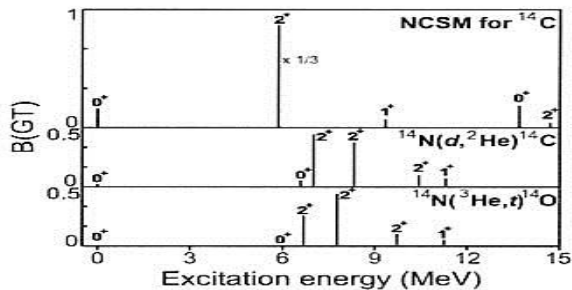
# Magnetic moments of p-shell nuclei



# B(GT) values for $^{14}\text{N} \rightarrow ^{14}\text{C}$



**present = SFO** Suzuki, Fujimoto, Otsuka, PR C67 (2003)



Negret et al., PRL 97 (2006)

KVI  
RCNP

**Space: up to 2-3 hw**

**SFO\*:**  $g_A^{\text{eff}}/g_A = 0.95$

**B(GT:  $^{12}\text{C}$ )\_cal = experiment**

FIG. 3. Experimental B(GT) distributions, compared to the theoretical result of Aroua *et al.* [14], where the B(GT) to the  $2^+$  state was scaled down by a factor of 3.

# New shell-model Hamiltonians in fp-shell and spin responses

**GXPF1:** Honma et al., PR C65 (2002); C69 (2004); A = 47-66

**KB3:** Caurier et al., Rev. Mod. Phys. 77, 427 (2005)

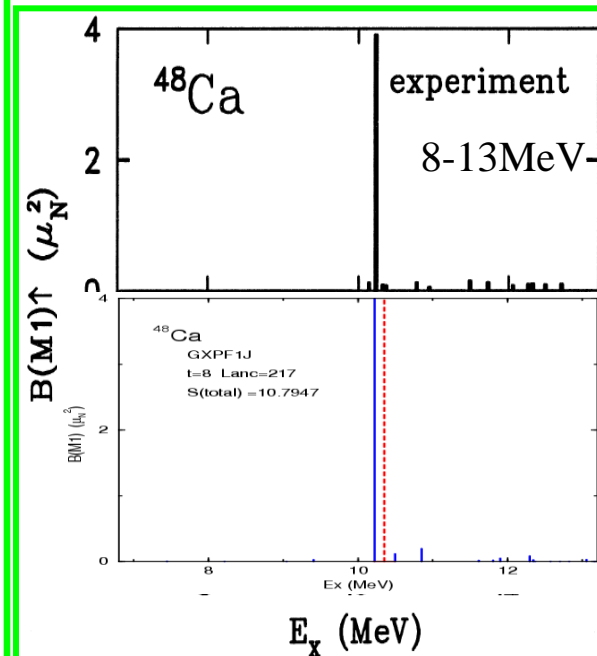
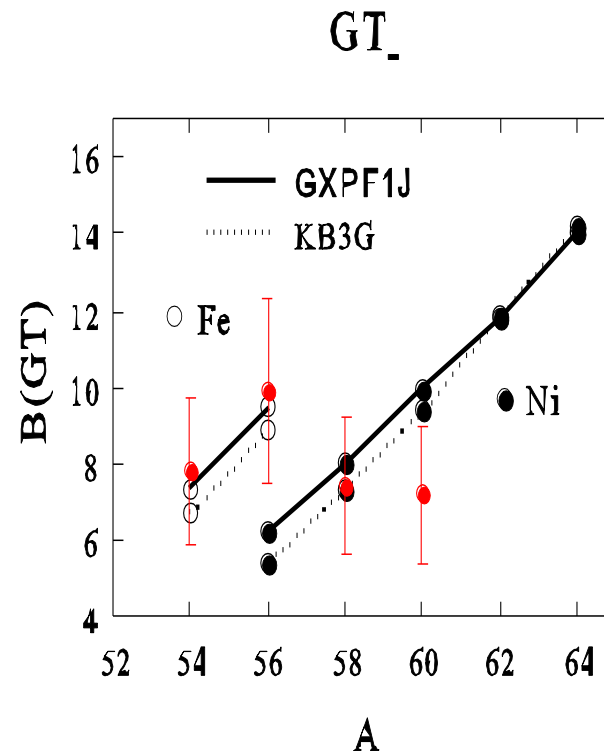
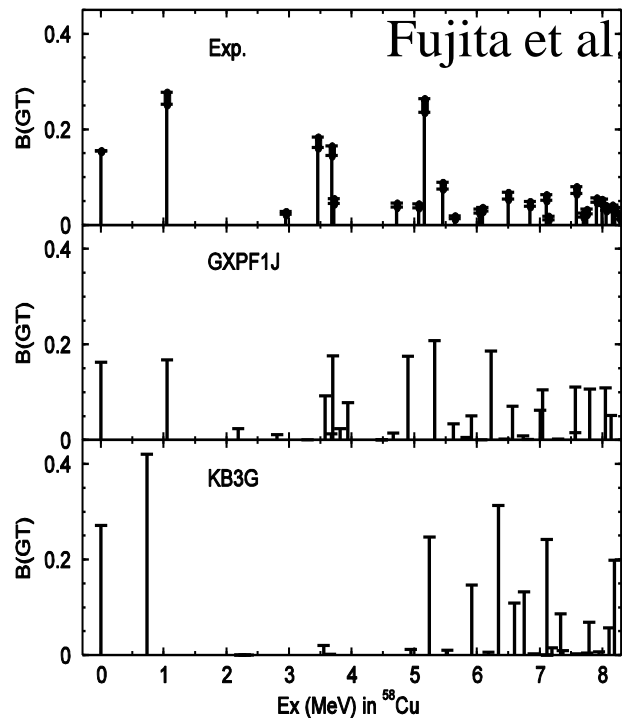
KB3G A = 47-52 KB + monopole corrections

- Spin properties of fp-shell nuclei are well described

B(GT<sub>-</sub>) for <sup>58</sup>Ni  $g_A^{\text{eff}}/g_A^{\text{free}}=0.74$

M1 strength  
(GXPF1J)

$g_S^{\text{eff}}/g_S=0.75 \pm 0.2$



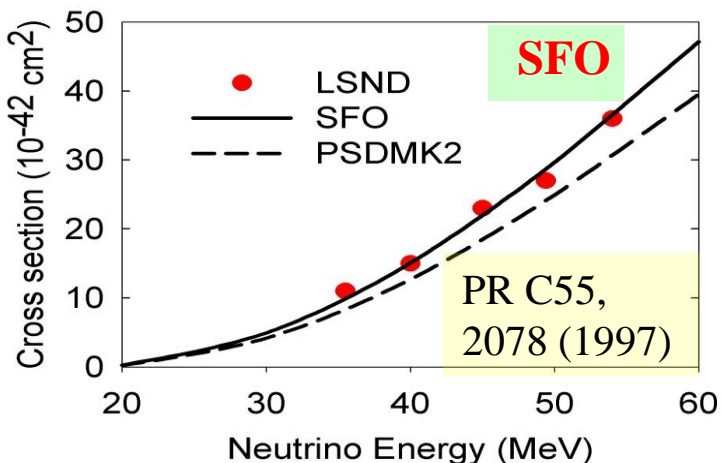
# ○ $\nu$ -nucleus reactions

p-shell: SFO

pf-shell: GXPF1J (Honma et al.)

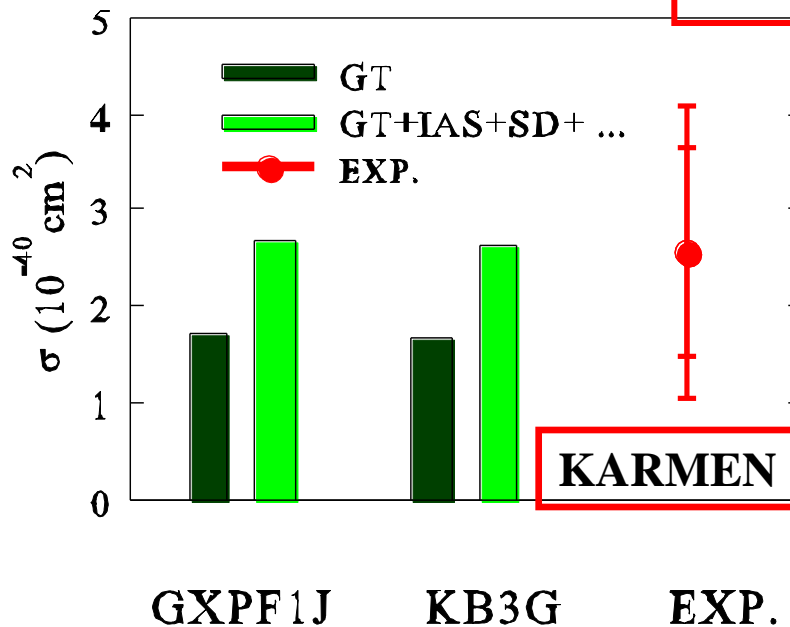
cf. KB3 Caurier et al.

**GT**  $^{12}\text{C} (\nu_e, e^-) ^{12}\text{N}_{\text{g.s.}}$



$^{56}\text{Fe}(\nu, e^-) ^{56}\text{Co}$

DAR



Suzuki, Chiba, Yoshida, Kajino, Otsuka, PR C74, 034307, (2006).

SFO:  $g_A^{\text{eff}}/g_A = 0.95$

B(GT:  $^{12}\text{C}$ )\_cal = experiment

$B(\text{GT})=9.5$   $B(\text{GT})_{\text{exp}}=9.9 \pm 2.4$   $B(\text{GT})_{\text{KB3G}}=9.0$

$(\nu, \nu')$ ,  $(\nu_e, e^-)$  SD exc.

SD + ... : RPA (SGII)

SFO reproduces DAR cross sections

$$\langle \sigma \rangle_{\text{exp}} = (256 \pm 108 \pm 43) \times 10^{-42} \text{ cm}^2$$

$$\langle \sigma \rangle_{\text{th}} = (258 \pm 57) \times 10^{-42} \text{ cm}^2$$

SM(GXPF1J)+RPA(SGII)  $259 \times 10^{-42} \text{ cm}^2$

RHB+RQRPA(DD-ME2) 263

RPA(Landau-Migdal force) 240

# Nucleosynthesis processes of light elements

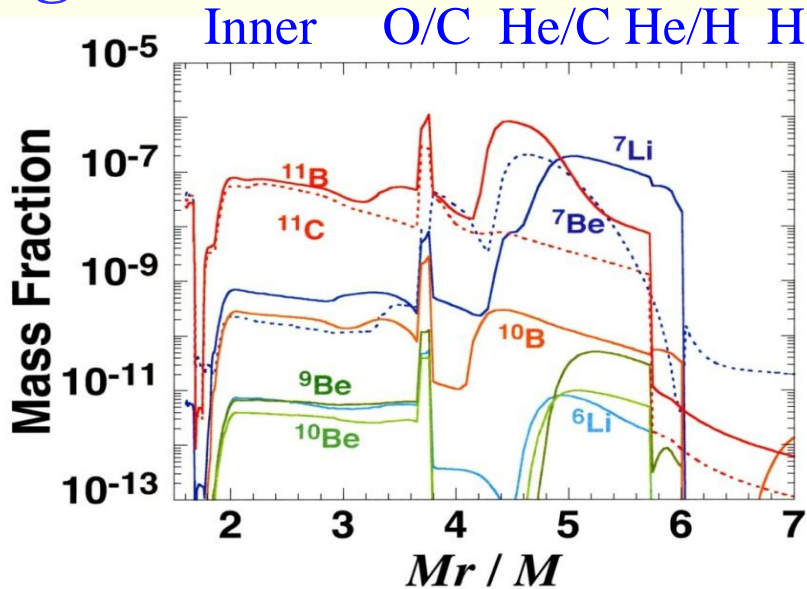
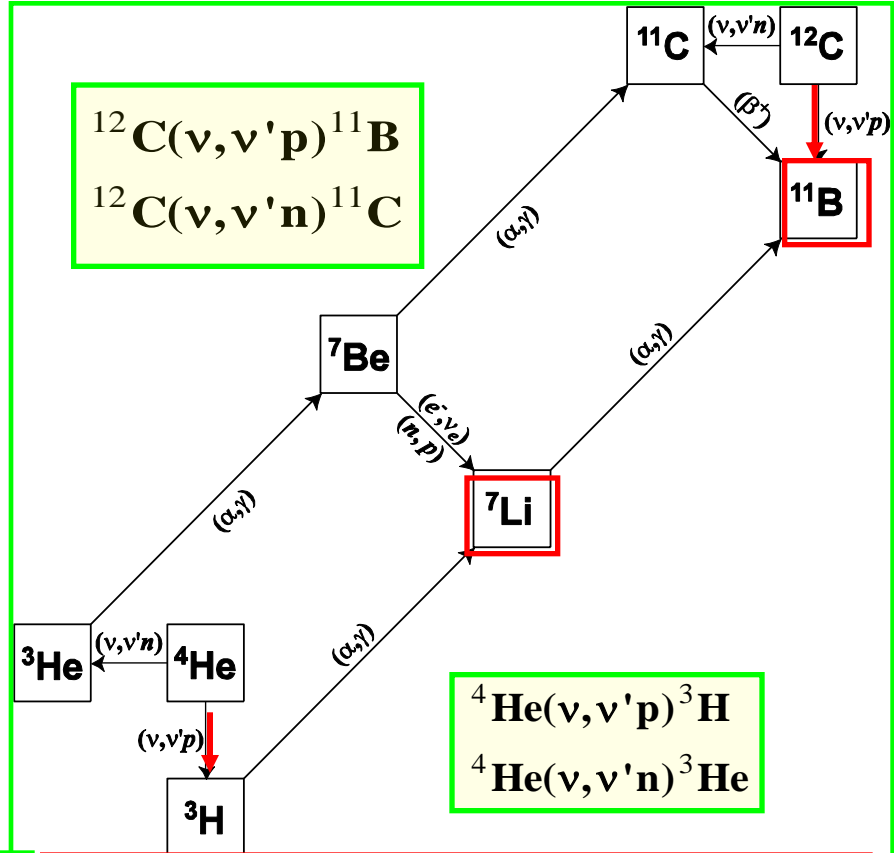
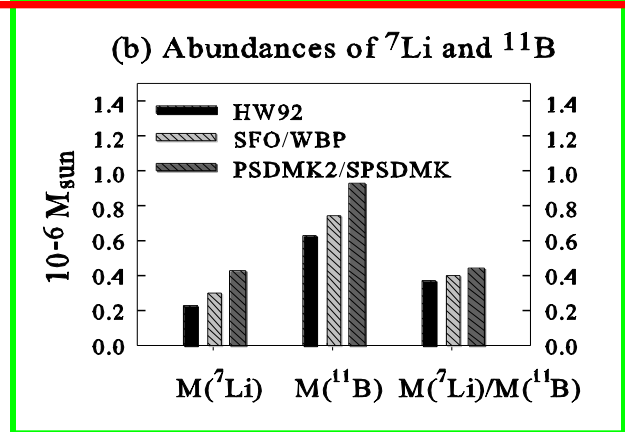
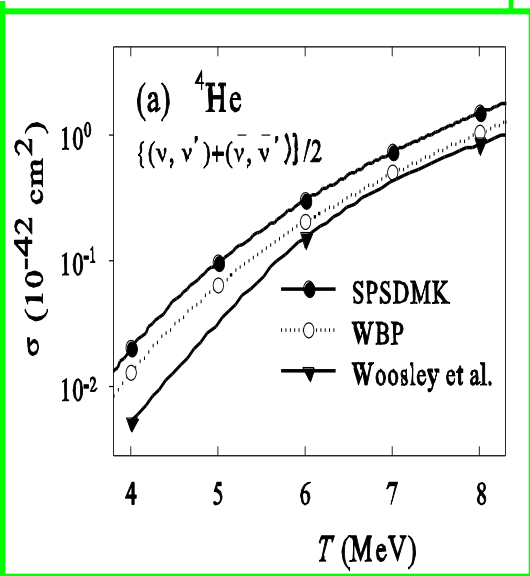
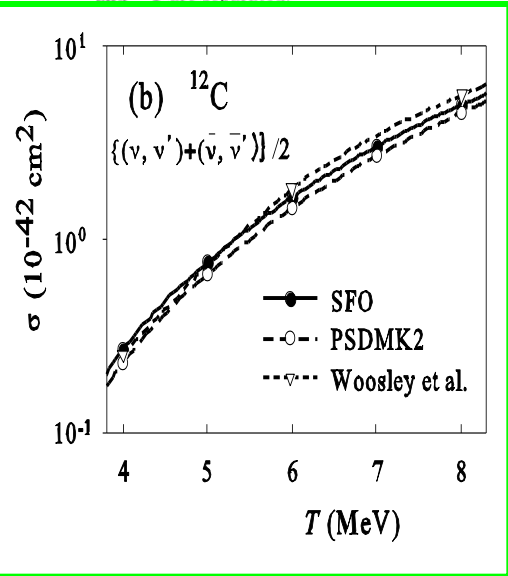


Fig. 4.— Mass fraction distribution of Model 1. The mass fractions of  ${}^7\text{Li}$  and  ${}^7\text{Be}$ , and  ${}^{11}\text{B}$  and  ${}^{11}\text{C}$  are separated.



Enhancement of  ${}^{11}\text{B}$  and  ${}^7\text{Li}$  abundances in supernova explosions

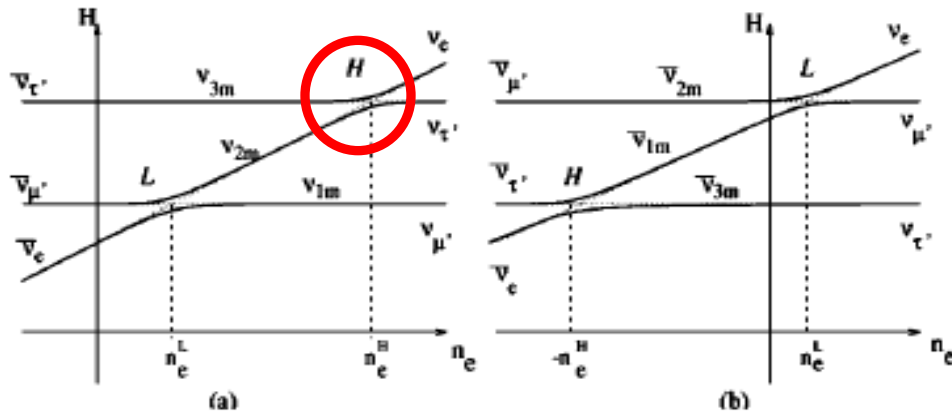




# MSW $\nu$ oscillations

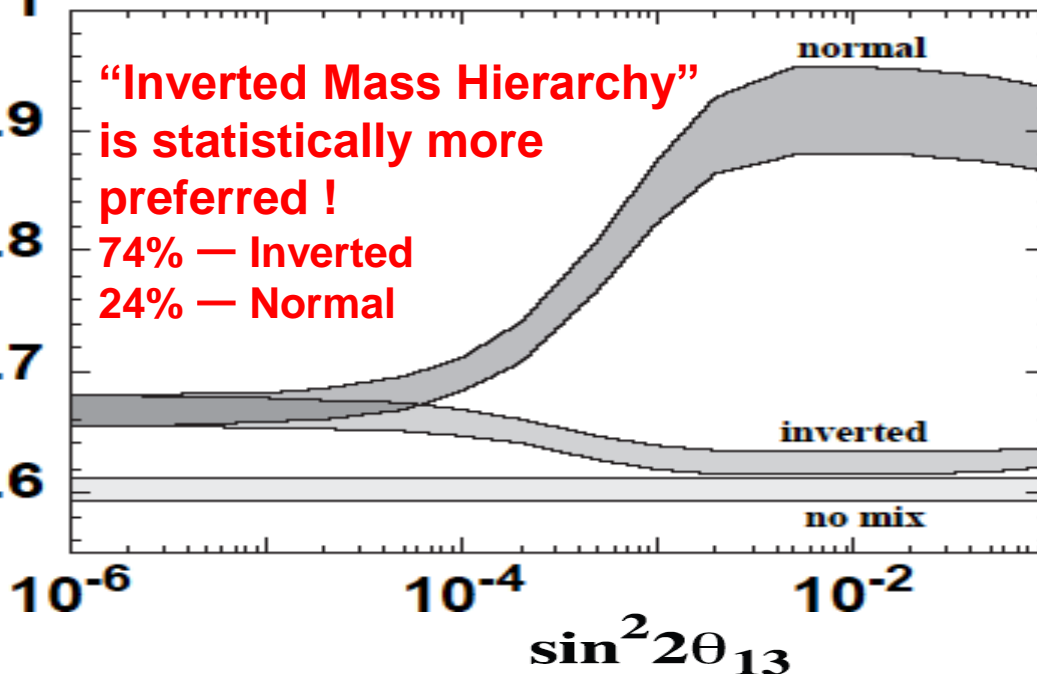
Normal hierarchy

Inverted hierarchy



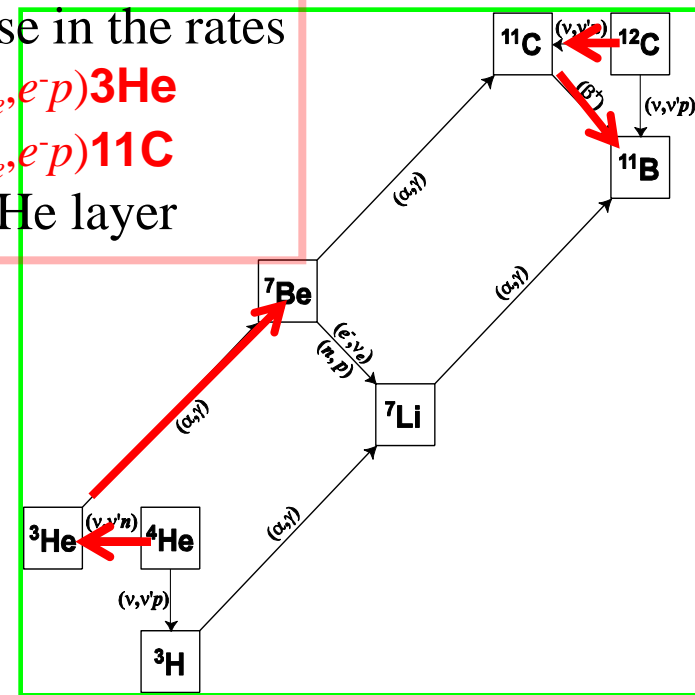
Normal – hierarchy :  $\nu_\mu, \nu_\tau \rightarrow \nu_e$

${}^7\text{Li}/{}^{11}\text{B}$ -Ratio



Increase in the rates

$4\text{He}(\nu_e, e^-p)3\text{He}$   
 $12\text{C}(\nu_e, e^-p)11\text{C}$   
 in the He layer



- T2K, MINOS (2011)
  - Double CHOOZ, Daya Bay, RENO (2012)
- $\sin^2 2\theta_{13} = 0.1$

First Detection of  ${}^7\text{Li}/{}^{11}\text{B}$  in SN-grains in Murchison Meteorite  
 W. Fujiya, P. Hoppe, & U. Ott, ApJ 730, L7 (2011).

Bayesian analysis:  
 Mathews, Kajino, Aoki and Fujiya, Phys. Rev. D85,105023 (2012).

- Effects of MSW  $\nu$ -oscillations

normal hierarchy: high res. + low res.  $\rightarrow$   ${}^7\text{Li}/{}^{11}\text{B}$  enhanced

inverted-hierarchy: no high-res.  $\rightarrow$   ${}^7\text{Li}/{}^{11}\text{B}$  not enhanced

### Supernova X-grains in Murchison meteorite

$\rightarrow$  inverted hierarchy is statistically favored

W. Fujiya, P. Hoppe, & U. Ott, ApJ 730, L7 (2011).

Mathews, Kajino, Aoki and Fujiya, Phys. Rev. D85,105023 (2012).

- New  $\nu$ - ${}^{13}\text{C}$  cross sections with SFO

${}^{13}\text{C}$  is a good target for low-energy  $\nu$  detection;  $E < 10$  MeV

Suzuki, Balantekin and Kajino, PR C86, 015502 (2012)

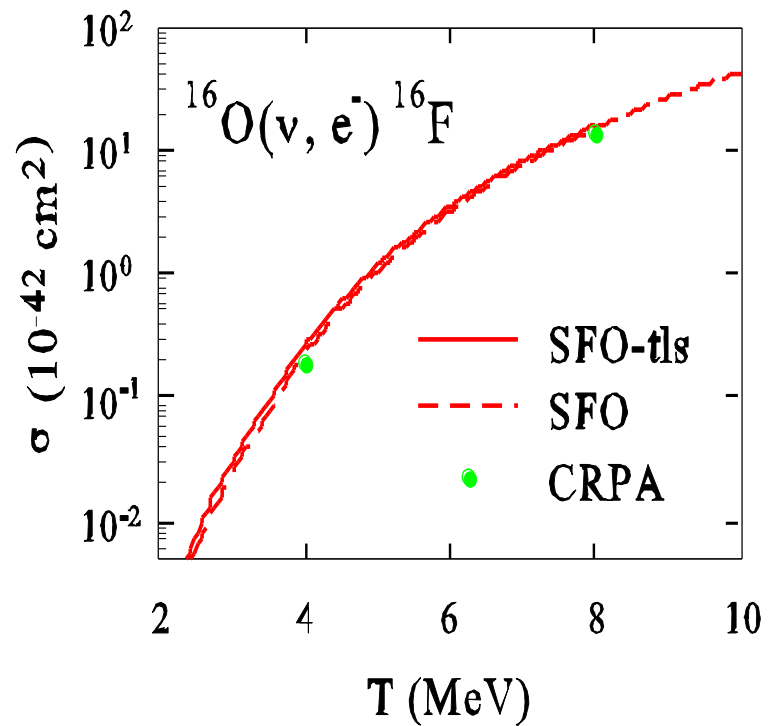
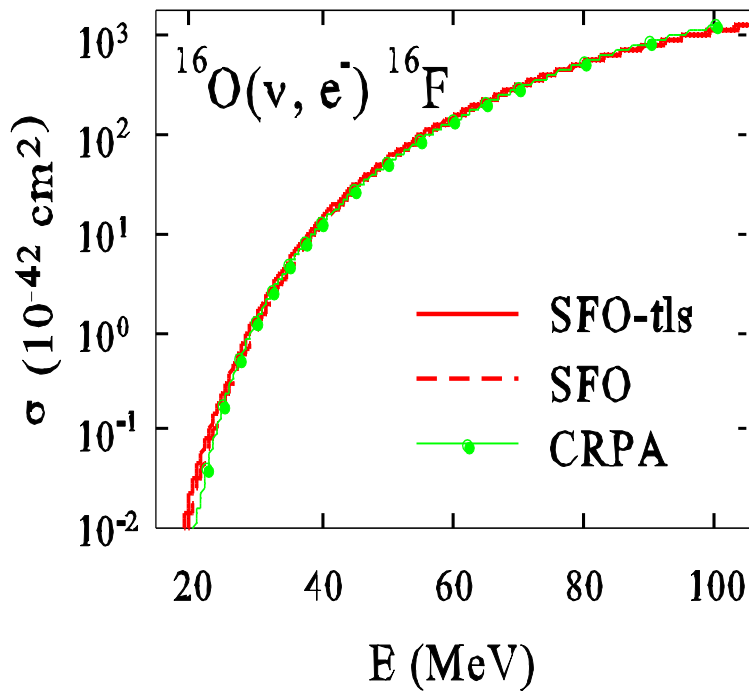
- New  $\nu$ - ${}^{16}\text{O}$  cross sections with SFO-tls

Full inclusion of tensor force in p-sd cross shells:

tensor  $\rightarrow$   $\pi + \rho$     LS  $\rightarrow$   $\sigma + \rho + \omega$

Spin-dipole transitions ( $0^-$ ,  $1^-$ ,  $2^-$ )

Excitation energies of the spin-dipole states are improved.

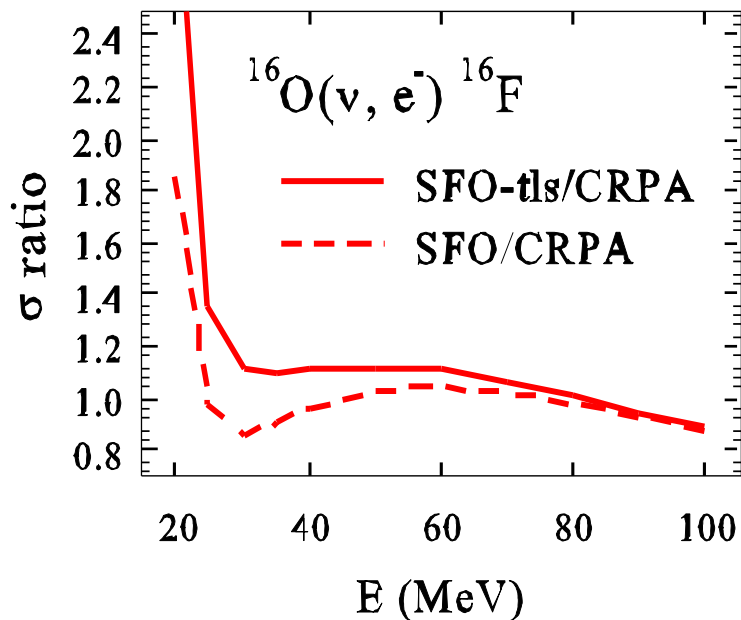


$T =$  temperature of supernova  $\nu$

$T$	$\sigma(\text{SFO-tls})/\sigma(\text{CRPA})$ :
4	1.41
8	1.17

$g_A^{\text{eff}}/g_A = 0.95$

CRPA: Kolbe, Langanke & Vogel, PR D66 (2002)



# Soft dipole resonance in $^{11}\text{Li}$

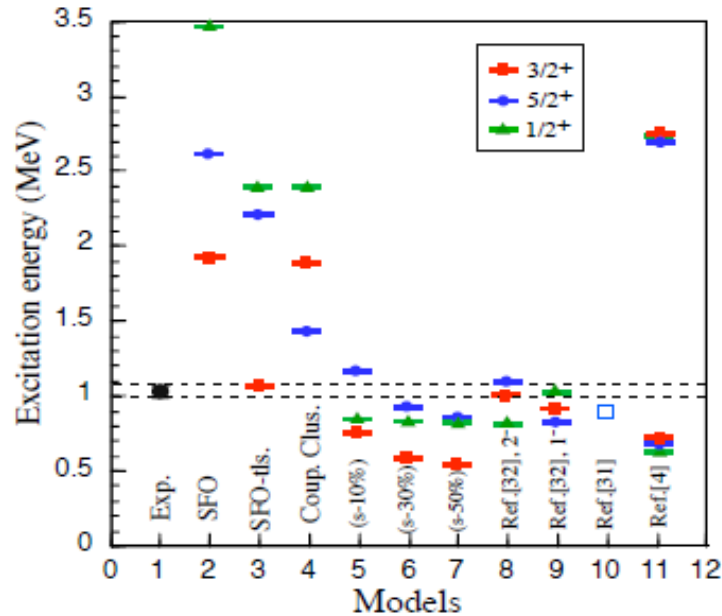
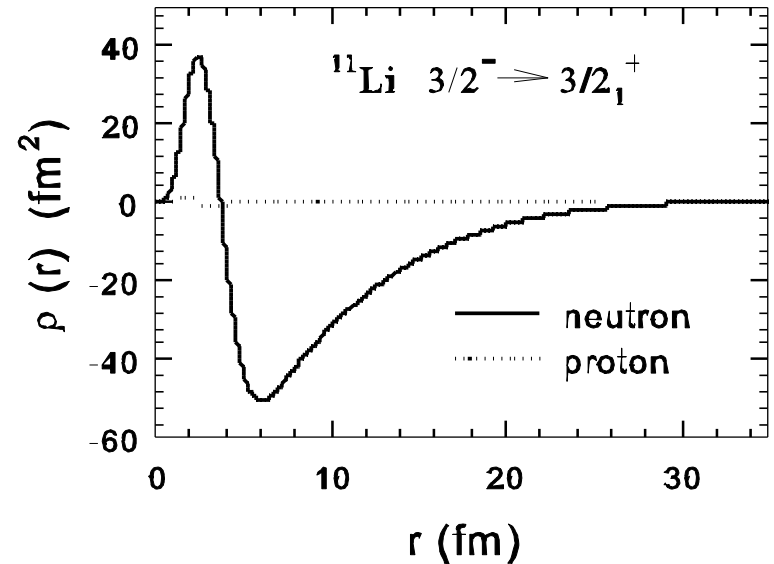


FIG. 4: The experimental excitation energy compared with different theoretical model predictions. 1=experimental data, Shell model with 2=SFO and 3=SFO-tls interactions, 4=Coupled Cluster, 5,6,7=three-body model with  $2s_{1/2}$ , 10%, 30% and 50%, respectively, 8=Ref.[32] with  $^{10}\text{Li}(2^-)$ , 9=Ref.[32] with  $^{10}\text{Li}(1^-)$ , 10=Ref.[31] and 11=Ref.[4]. The red (squares), blue (circles), green (triangles) lines represent states with spin  $3/2^+$ ,  $5/2^+$ ,  $1/2^+$ , respectively.

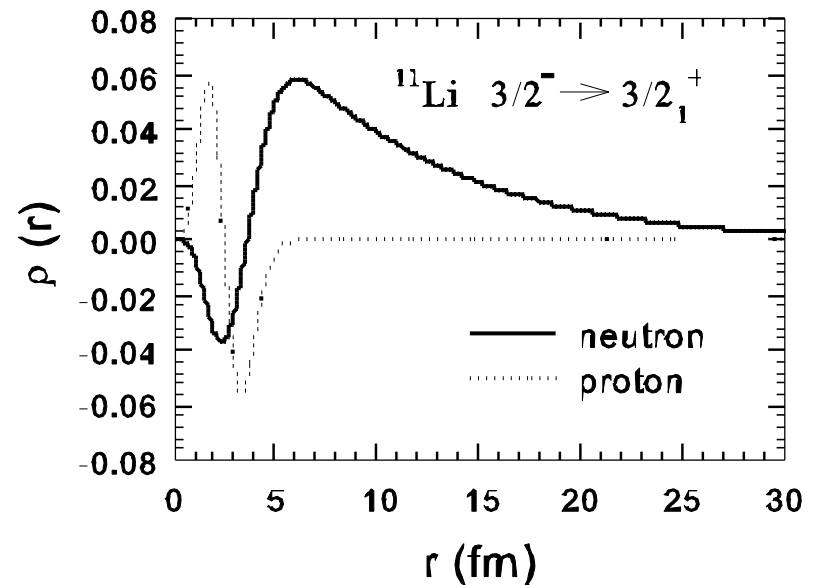
$$^{11}\text{Li} (d, d') \ ^{11}\text{Li}$$

Kanungo et al., PRL, in press

## Isoscalar E1 transition density



## IV E1 transition density



# ▪ $\nu$ - $^{40}\text{Ar}$ reactions

Liquid argon = powerful target for SN $\nu$  detection

VMU= Monopole-based universal interaction

tensor force: bare  $\approx$  renormalized

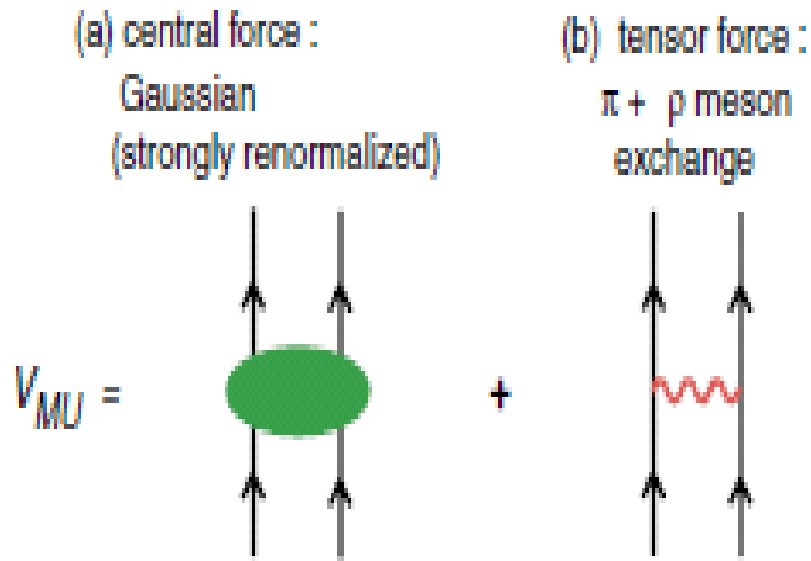


FIG. 2 (color online). Diagrams for the  $V_{MU}$  interaction.

○ sd-pf shell:  $^{40}\text{Ar}(\nu, e^-)^{40}\text{K}$

SDPF-VMU-LS

sd: SDPF-M (Utsuno et al.)

fp: GXPF1 (Honma et al.)

sd-pf: VMU + 2-body LS

(sd) $^{-2}$  (fp) $^2$  : 2hw

B(GT) &  $\nu$ - $^{40}\text{Ar}$  cross sections

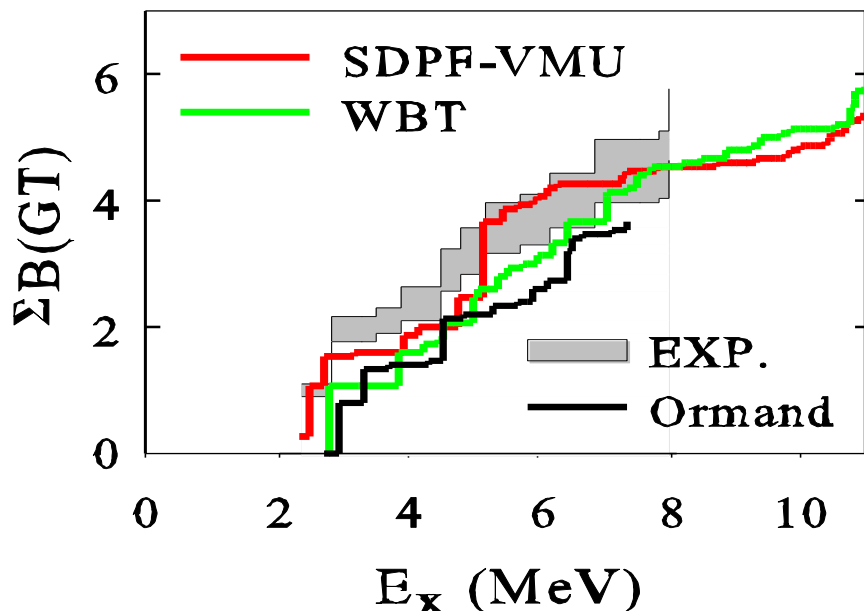
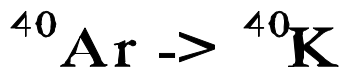
Solar  $\nu$  cross sections folded over

$^8\text{B}$   $\nu$  spectrum

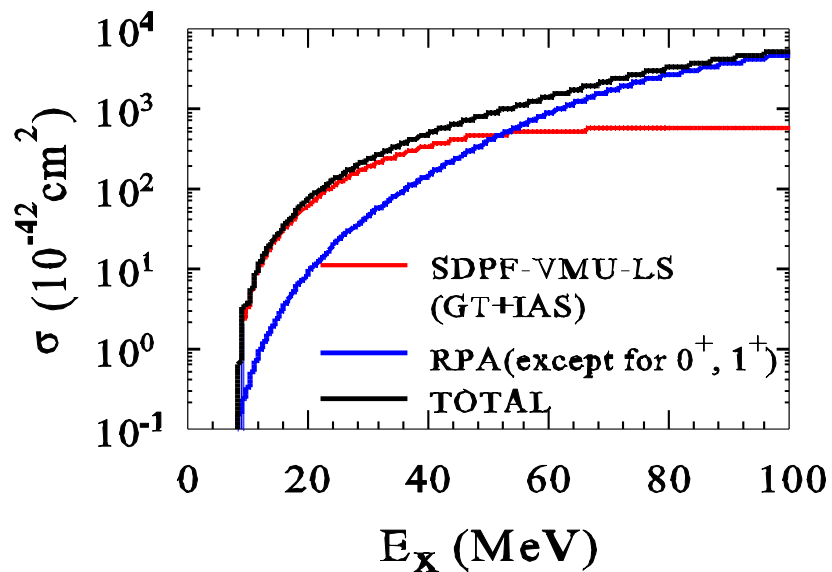
## Important roles of tensor force

Otsuka, Suzuki, Honma, Utsuno,  
Tsunoda, Tsukiyama, Hjorth-Jensen  
PRL 104 (2010) 012501

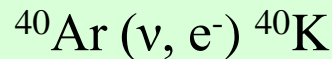
Suzuki and Honma, PR C87, 014607 (2013)



(p,n) Bhattacharya et al., PR C80 (2009)

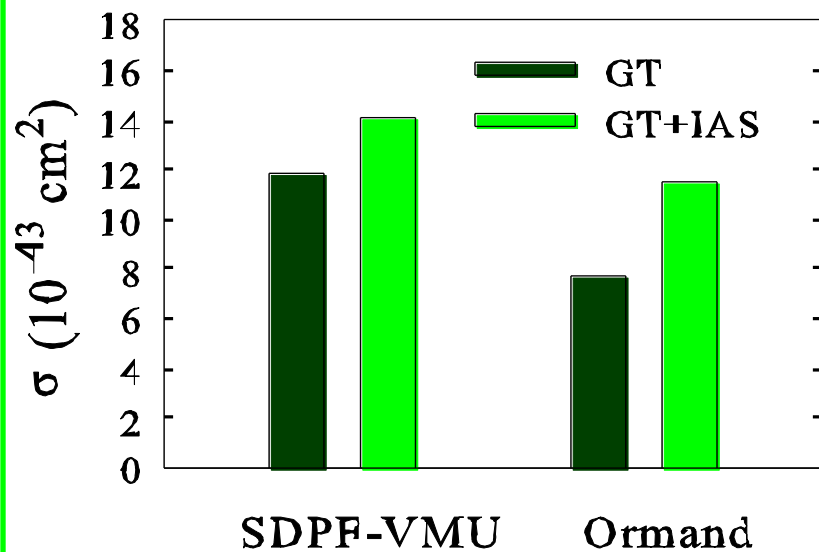
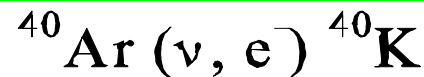


Solar  $\nu$  cross sections folded over  $^8\text{B}$   $\nu$  spectrum



GT+IAS

$E_e > 5$  MeV : ICARUS



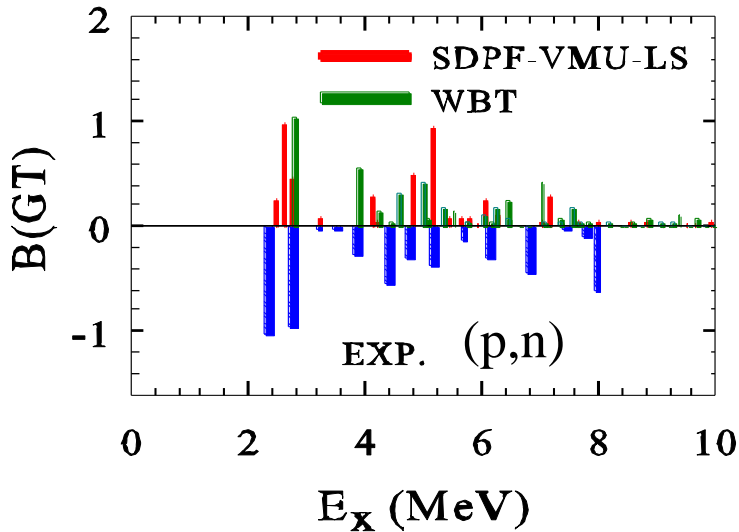
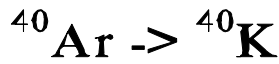
IAS:  $C_0 + L_0 \approx [(q^2 - \omega^2)/q^2]^2 \times C_0$ ; +  $C_0$  only

GT:  $E_1^5 + M_1 + C_1^5 + L_1^5$ ; +  $E_1^5$  only

+Ormand et al, PL B345, 343 (1995)

Gamow-Teller transitions in the  $A = 40$  isoquintet of relevance for neutrino captures in  $^{40}\text{Ar}$ 

M. Karakoç,<sup>1,2</sup> R. G. T. Zegers,<sup>3,4,5,\*</sup> B. A. Brown,<sup>3,4,5</sup> Y. Fujita,<sup>6,7</sup> T. Adachi,<sup>6</sup> I. Boztosun,<sup>1,2</sup> H. Fujita,<sup>6</sup> M. Csatlós,<sup>8</sup> J. M. Deaven,<sup>3,4,5,†</sup> C. J. Guess,<sup>3,4,5,‡</sup> J. Gulyás,<sup>8</sup> K. Hatanaka,<sup>6</sup> K. Hirota,<sup>6</sup> D. Ishikawa,<sup>6</sup> A. Krasznahorkay,<sup>8</sup> H. Matsubara,<sup>6,8</sup> R. Meharchand,<sup>3,4,5,‡</sup> F. Molina,<sup>9,8</sup> H. Okamura,<sup>6,\*\*,</sup> H. J. Ong,<sup>6</sup> G. Perdikakis,<sup>3,4,5,††</sup> C. Scholl,<sup>10,‡‡</sup> Y. Shimbara,<sup>11,88</sup> G. Susoy,<sup>12</sup> T. Suzuki,<sup>6</sup> A. Tamii,<sup>6</sup> J. H. Thies,<sup>13</sup> and J. Zenihiro<sup>6,11</sup>



$$R = \frac{B(\text{GT})_{2730 \text{ keV}}}{B(\text{GT})_{2290 \text{ keV}}}, \quad R=0.48$$

TABLE I. Experimental and shell-model  $B(\text{GT})$  values and their ratios for the transitions to the  $1^+$  states at 2290 and 2730 keV.

$E_x(^{40}\text{K})$ (keV)	$B(\text{GT})_{\text{exp}}$			$B(\text{GT})_{\text{SM}}^d$	
	$(p,n)^a$	$\beta(^{40}\text{Ti})^b$	$(^3\text{He},t)^c$	$^{40}\text{Ar} \rightarrow ^{40}\text{K}$	$^{40}\text{Ti} \rightarrow ^{40}\text{Sc}$
2289.87(1)	1.03(10)	0.57(3)	—	0.97	0.40
2730.37(2)	0.94(9)	0.94(4)	—	0.42	0.94
$R$	0.911(5)	1.65(11)	0.73(5)	0.43	2.35

<sup>a</sup>From Ref. [10].

<sup>b</sup>From Ref. [9] and using isospin symmetry.

<sup>c</sup>Only the relative strengths for the two states are known experimentally.

<sup>d</sup>The shell-model calculations have been multiplied by a factor 0.60 to account for quenching of the GT strength [16].

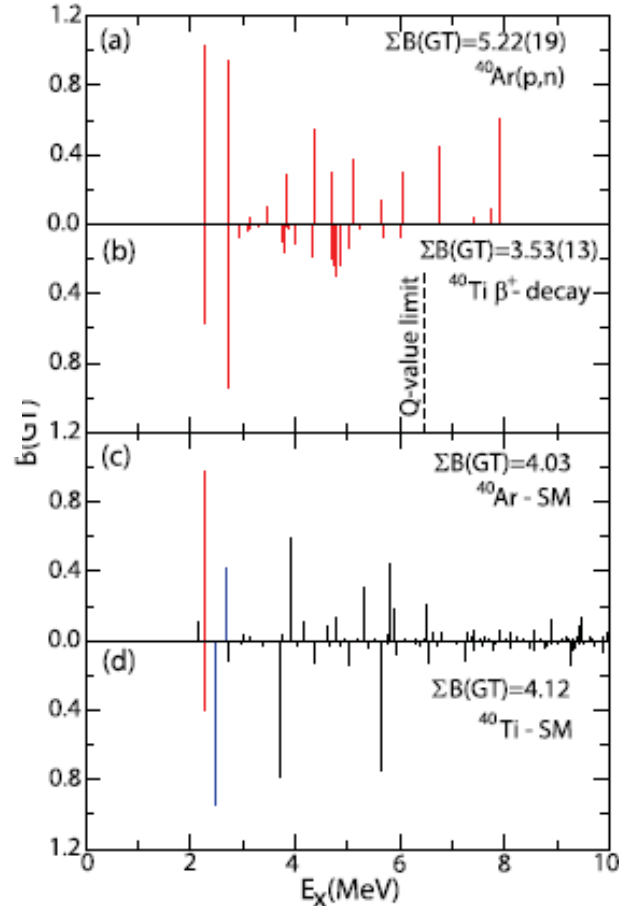


FIG. 1. (Color online) GT strength distributions in the  $A = 40$ ,  $T = 2$  isoquintet. (a) Extracted from  $^{40}\text{Ar}(p,n)$  [10]. (b) Extracted from  $\beta^+$  decay of  $^{40}\text{Ti}$ . The dashed line indicates the limit of the  $Q$ -value window available for  $\beta^+$  decay. (c) Shell-model calculations for transitions from  $^{40}\text{Ar}$  to  $^{40}\text{K}$ . (d) Shell-model calculations for transitions from  $^{40}\text{Ti}$  to  $^{40}\text{Sc}$ .

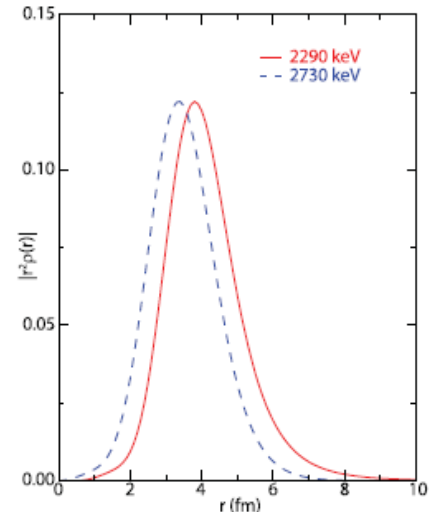


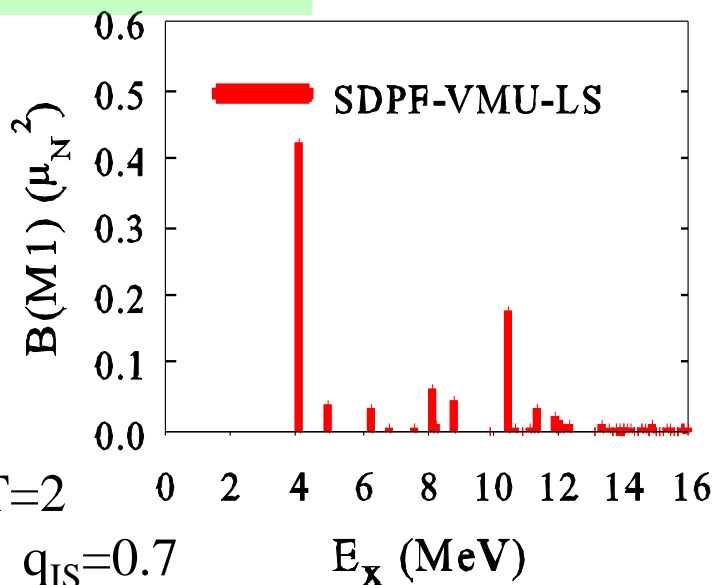
FIG. 3. (Color online) Radial transition densities (multiplied by  $r^2$ ) for the transitions from  $^{40}\text{Ar}$  to the  $1^+$  states at 2290 and 2730 keV. The vertical scales have been arbitrarily adjusted so that the peak values of the curves are equal.

WBMB-C

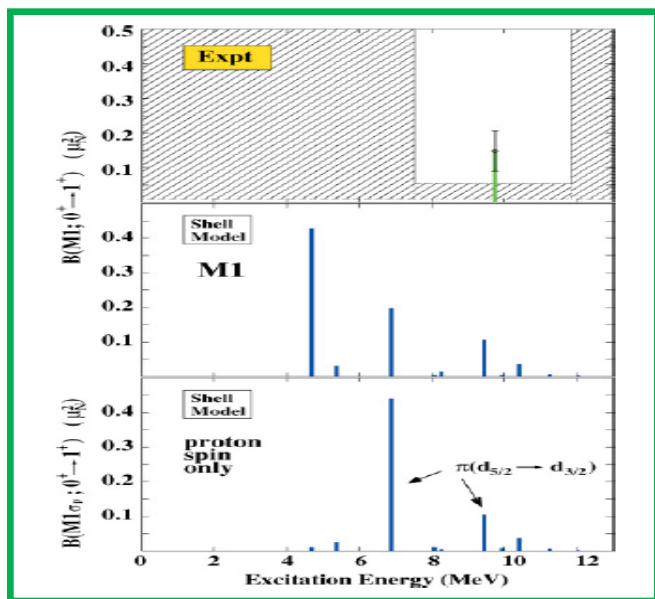
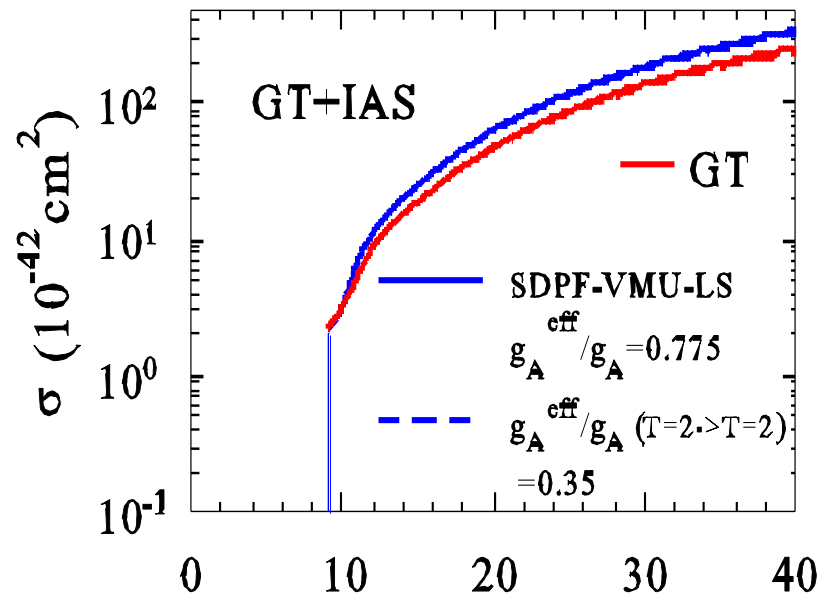
# Neutral-current

$^{40}\text{Ar}$

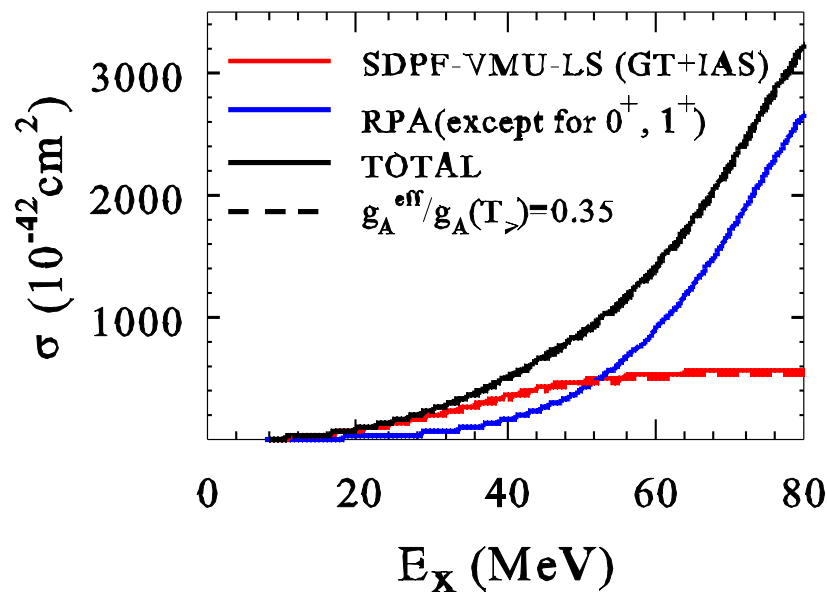
M1



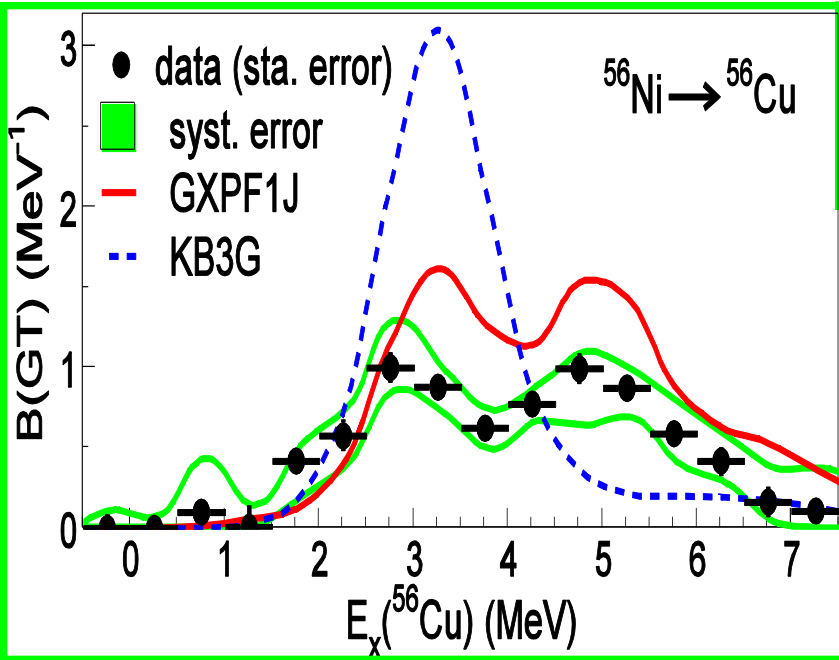
$^{40}\text{Ar} \rightarrow ^{40}\text{K}$



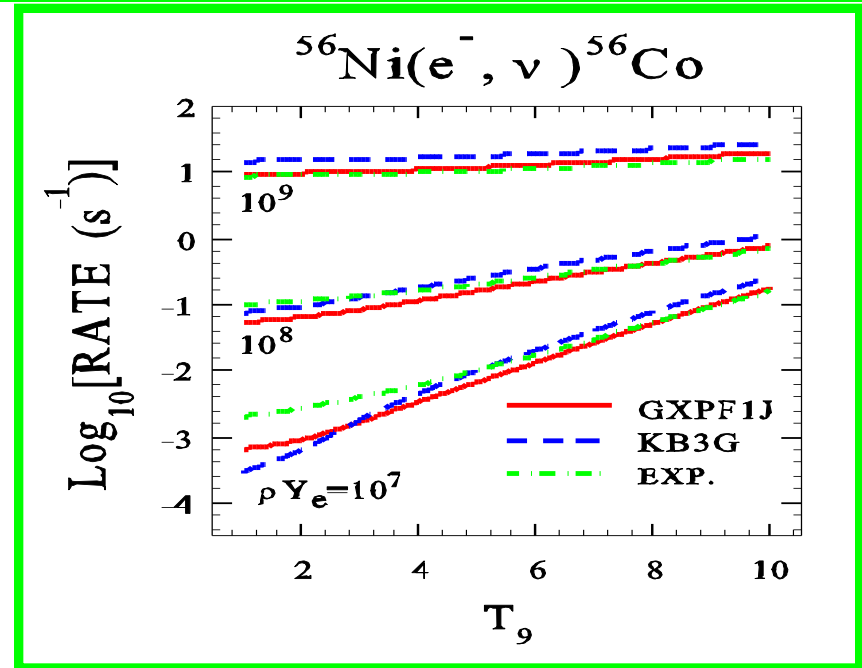
Exp.  $B(M1)=0.148(59) \mu_N^2$   
 Li et al, PR C73, 054306 (2006)







▪ e-capture rates on  $^{56}\text{Ni}$  in stellar environments:  $\rho Y_e = 10^7 [-10^{10} \text{ g/cm}^3]$



Sasano et al., PRL 107, 202501 (2011)

Suzuki, Honma, Mao, Otsuka, Kajino, PR C83, 044619 (2011)

## Type-Ia supernova explosion

Accretion of matter to white-dwarf from binary star

→ supernova explosion when white-dwarf mass >

Chandrasekhar limit

→  $^{56}\text{Ni}$  (N=Z)

→  $^{56}\text{Ni} (e^-, \nu) ^{56}\text{Co}$   $Y_e = 0.5 \rightarrow Y_e < 0.5$  (neutron-rich)

→ production of neutron-rich isotopes; more  $^{58}\text{Ni}$

Decrease of e-capture rate on  $^{56}\text{Ni}$

→ less production of  $^{58}\text{Ni}$ .

e-capture rates:

GXPF1J < KB3G

←→

$Y_e$  (GXPF1J) >  $Y_e$  (KB3G)

**Problem of over-production of  $^{58}\text{Ni}$  may be solved.**

# Problem of over-production of $^{58}\text{Ni}$

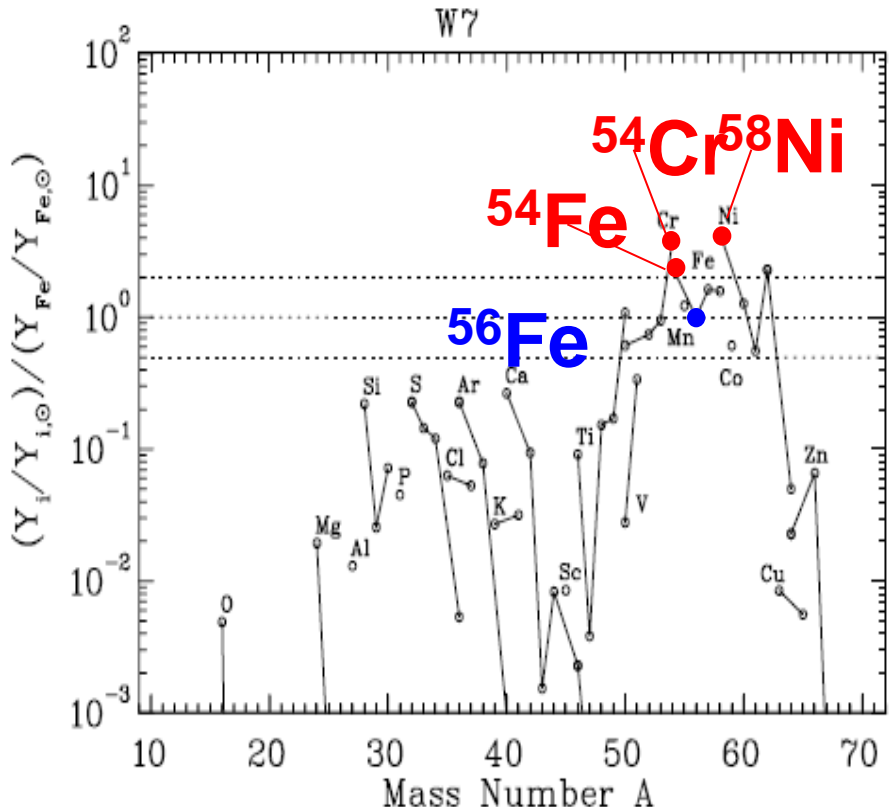
THE ASTROPHYSICAL JOURNAL SUPPLEMENT SERIES, 125:439-462, December

NUCLEOSYNTHESIS IN CHANDRASEKHAR MASS MODELS FOR TYPE Ia SUPERNOVAE AND CONSTRAINTS ON PROGENITOR SYSTEMS AND BURNING-FRONT PROPAGATION

KOICHI IWAMOTO,<sup>1,2,3</sup> FRANZISKA BRACHWITZ,<sup>4</sup> KEN'ICHI NOMOTO,<sup>1,2,3</sup> NOBUHIRO KISHIMOTO,<sup>1</sup>  
HIDEYUKI UMEDA,<sup>2,3</sup> W. RAPHAEL HIX,<sup>3,5</sup> AND FRIEDRICH-KARL THIELEMANN<sup>3,4,5</sup>

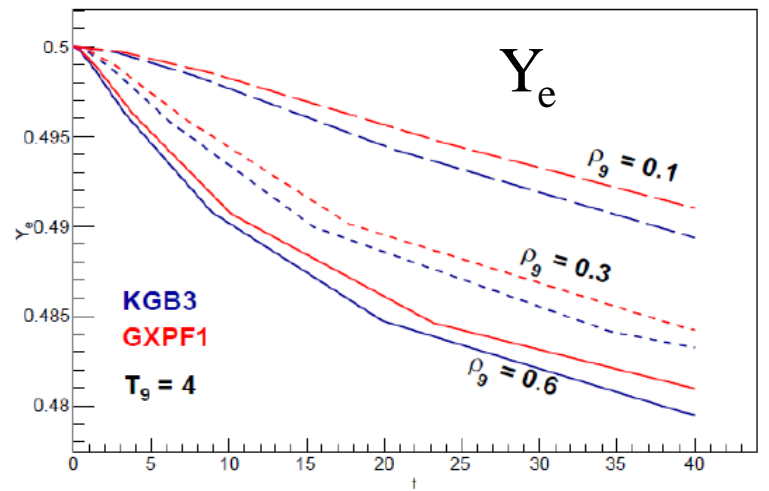
Received 1999 January 11; accepted 1999 July 29

and ignition densities to put new constraints on the above key quantities. The abundance of the Fe group, in particular of neutron-rich species like  $^{48}\text{Ca}$ ,  $^{50}\text{Ti}$ ,  $^{54}\text{Cr}$ ,  $^{54,58}\text{Fe}$ , and  $^{58}\text{Ni}$ , is highly sensitive to the electron captures taking place in the central layers. The yields obtained from such a slow central



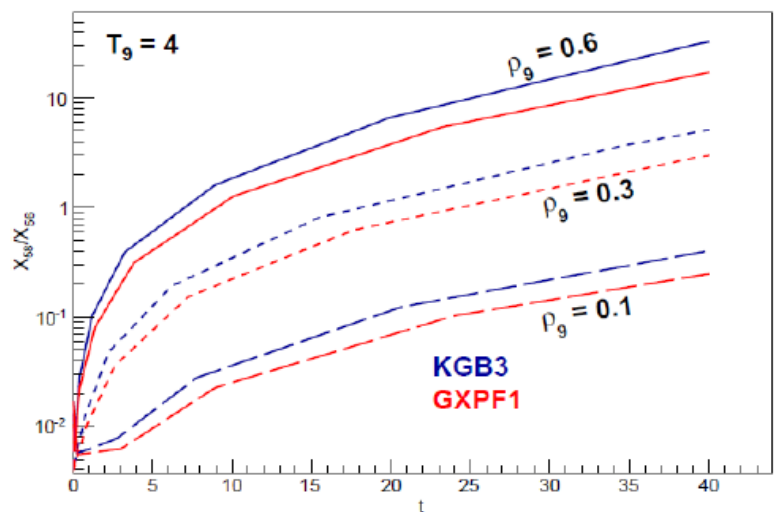
Famiano

# NSE(Nuclear Statistical Equilibrium) calculation

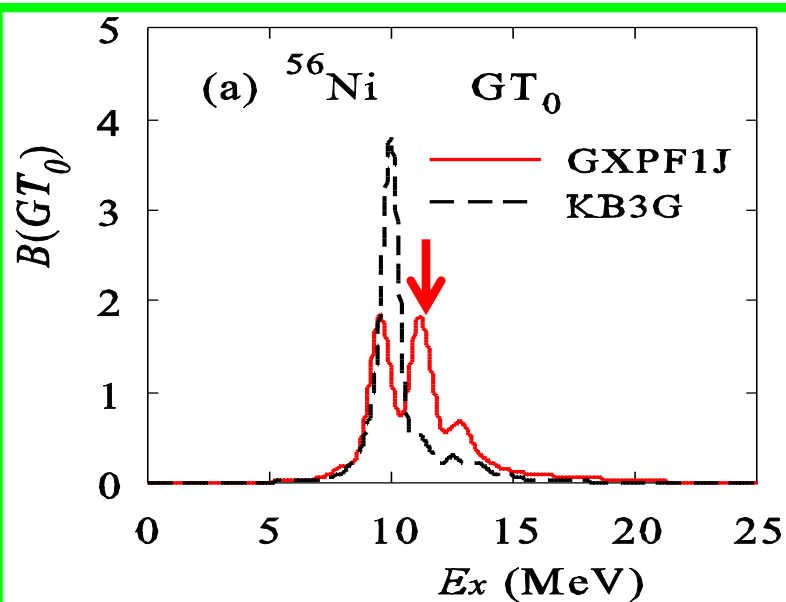


Ratio between  $^{58}\text{Ni} / ^{56}\text{Ni}$

GXPF1  $\rightarrow$   $^{58}\text{Ni}/^{56}\text{Ni}$  decreases

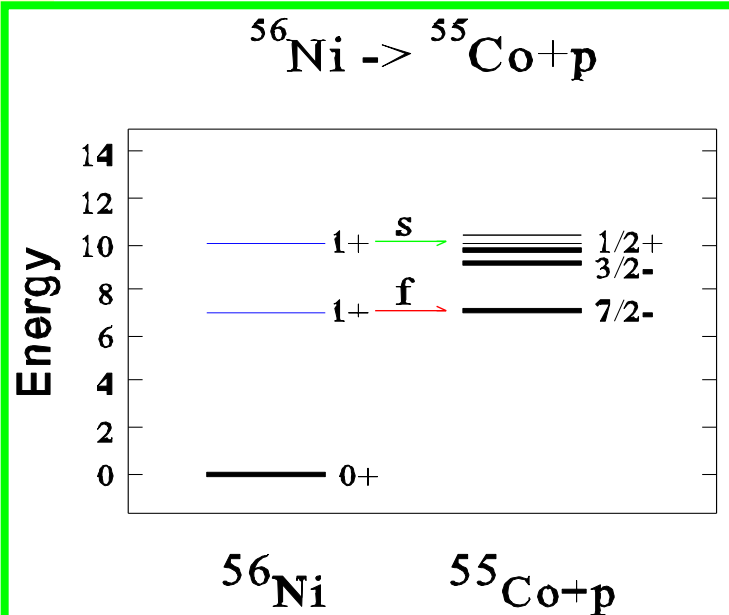


# Neutral current reaction on $^{56}\text{Ni}$

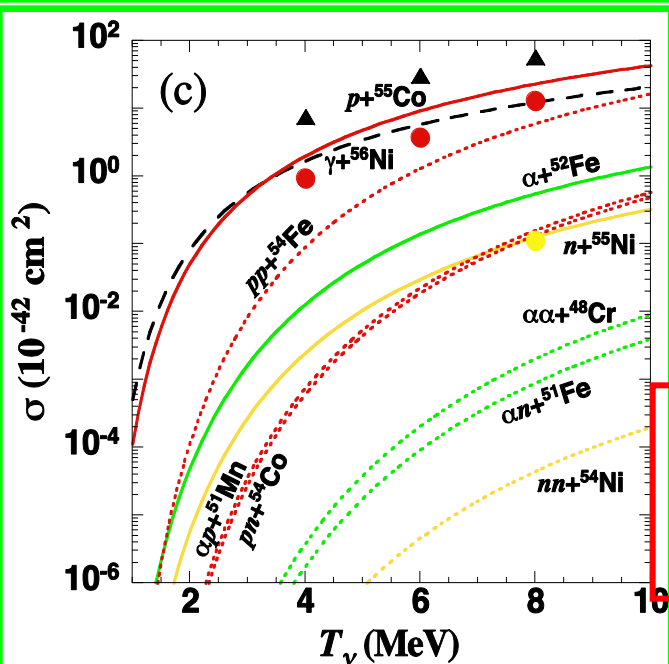


$B(\text{GT})=6.2$   
(GXPF1J)  
 $B(\text{GT})=5.4$   
(KB3G)

p-emission  
BR increases



## Synthesis of Mn in Population III Star

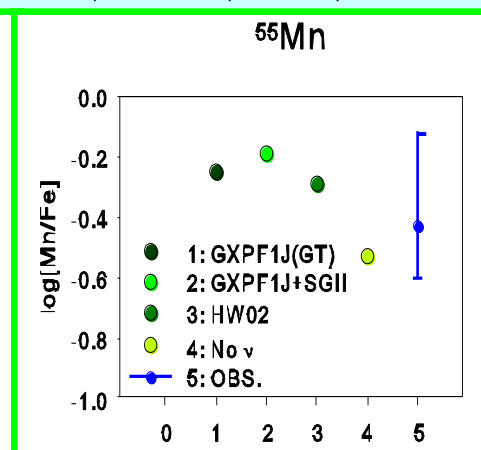
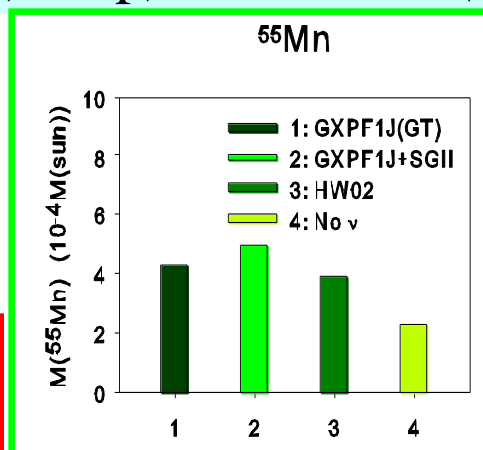


p-emission  
x-sections  
increase

cf:  $^{56}\text{Ni}(\nu, \nu' p) ^{55}\text{Co}$ ,  $^{55}\text{Co}(e^-, \nu) ^{55}\text{Fe}(e^-, \nu) ^{55}\text{Mn}$

HW02

▲ gamma  
● p  
● n

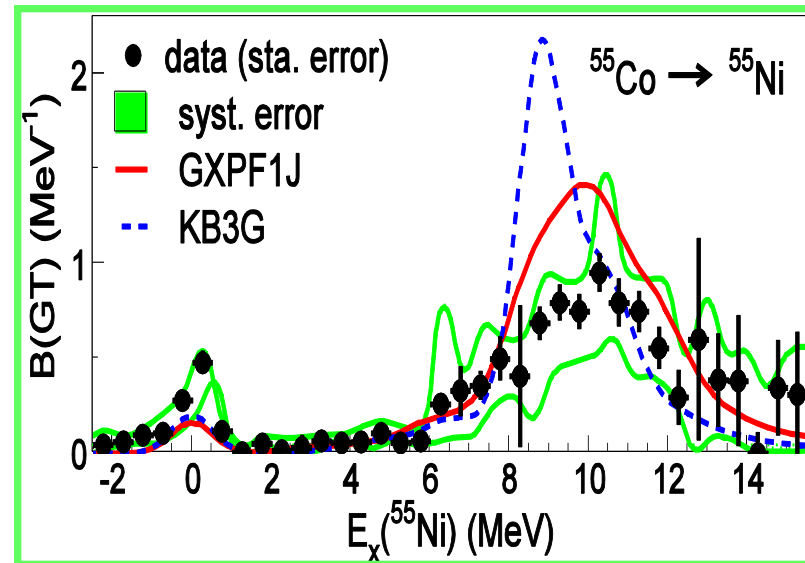


$^{54}\text{Fe}(p, \gamma) ^{55}\text{Co}$

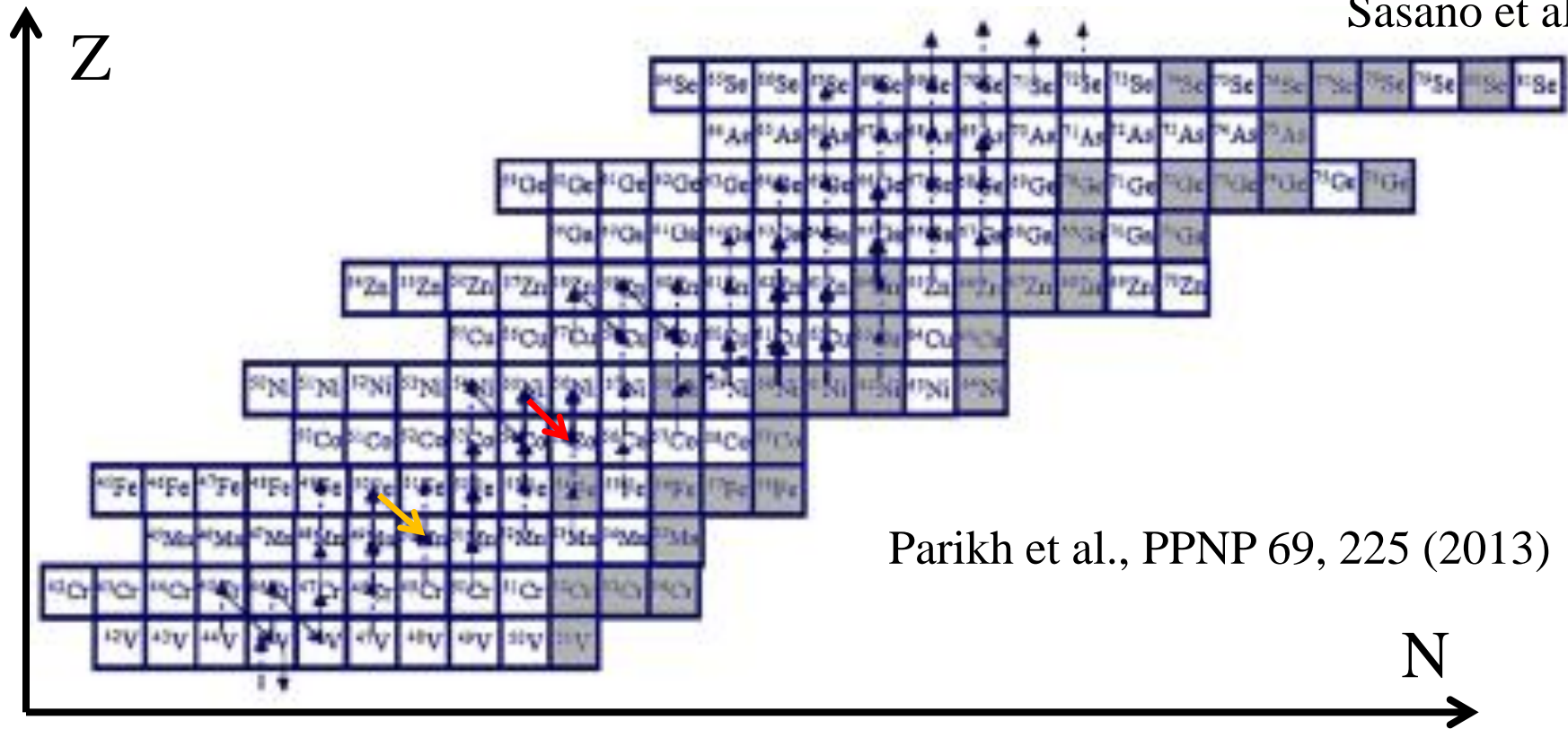
Yoshida, Umeda,  
Nomoto

# rp-process and X-ray burst

$(p, \gamma)$  &  $\beta^+$ -decay/e-capture



Sasano et al.



Parikh et al., PPNP 69, 225 (2013)

# X-ray burst



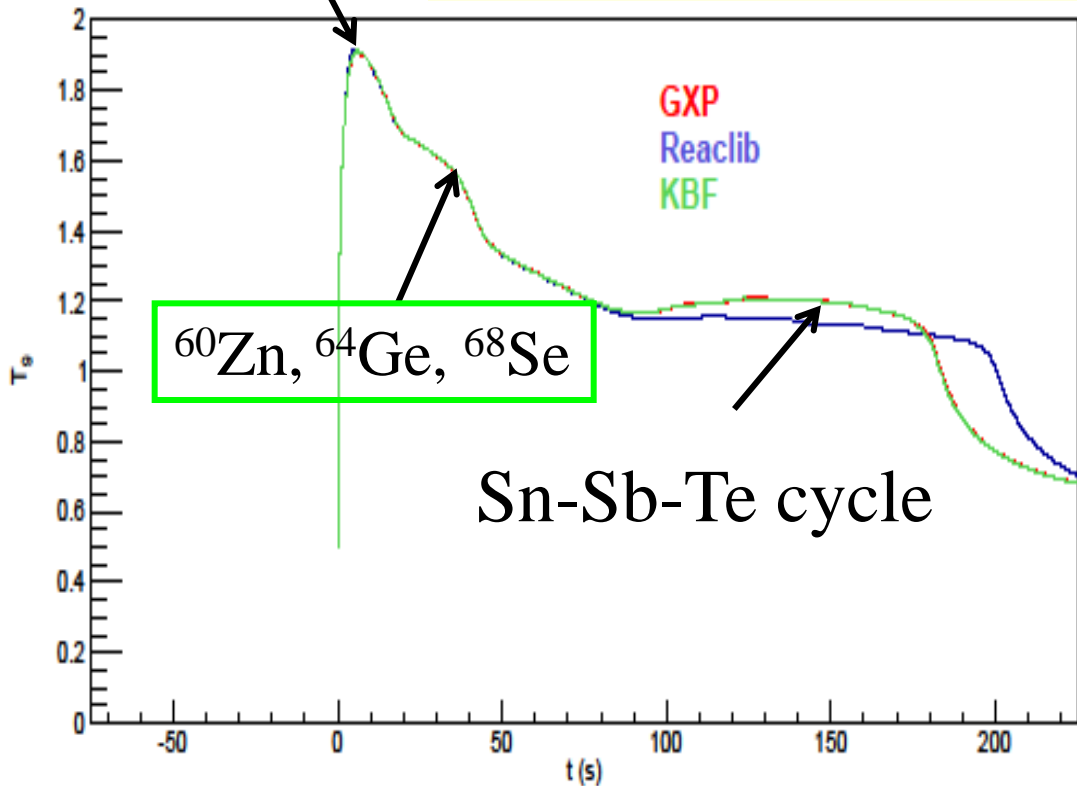
GXP\_rp.mov



KBF\_rp.mov

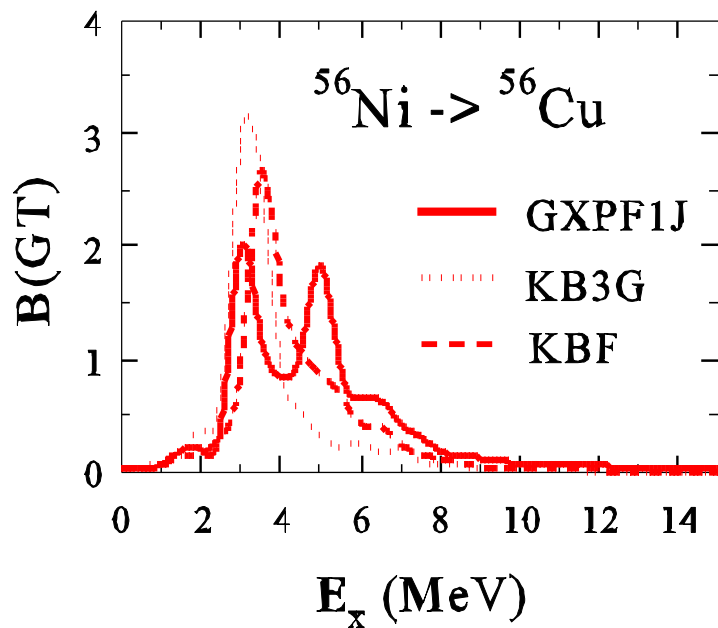
e-capture and beta-decay rates with KBF:  
 Langanke and Martinez-Pinedo,  
 Atomic Data and Nuclear Data  
 Tables **79**, 1 (2001)

$^{56}\text{Ni}$



Sn-Sb-Te cycle

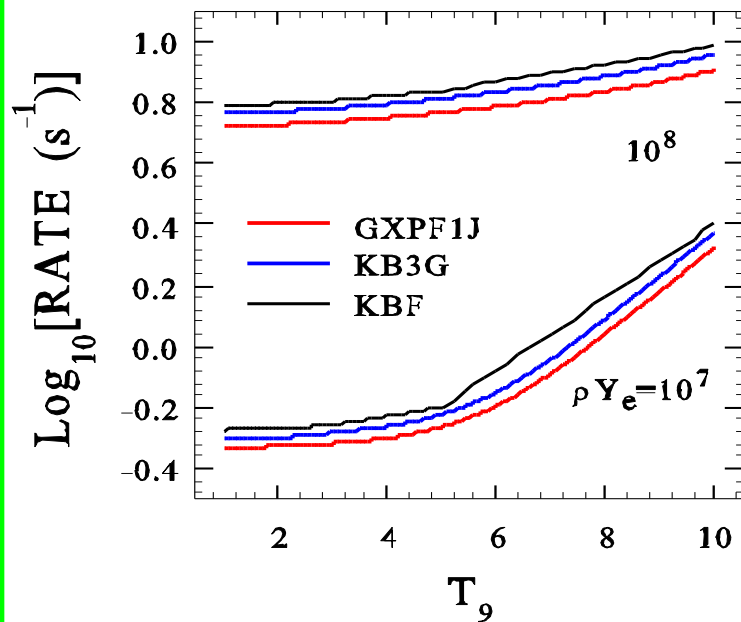
Famiano



$^{56}\text{Ni} \rightarrow ^{56}\text{Cu}$

— GXP  
 ..... KB3G  
 - - - KBF

$^{55}\text{Ni}(e^-, \nu) ^{55}\text{Co}$



$10^8$

$\rho Y_e = 10^7$

— GXP  
 — KB3G  
 — KBF

# Electron-capture and $\beta$ -decay rates at stellar environments

## ○ Evolution of $8\text{-}10M_{\odot}$ stars and nuclear URCA processes

- $M=0.5 \sim 8M_{\odot}$  : He burning  $\rightarrow$  C-O core  $\rightarrow$  C-O white dwarfs
- $M > 10M_{\odot}$  :  $\rightarrow$  Fe core  $\rightarrow$  core-collapse supernova explosion
- $M=8M_{\odot} \sim 10M_{\odot}$  : C burning  $\rightarrow$  O-Ne-Mg core
  - $\rightarrow$  (1) O-Ne-Mg white dwarf (WD)
  - $\rightarrow$  (2) e-capture supernova explosion (collapse of O-Ne-Mg core induced by e-capture) with neutron star (NS) remnant
  - $\rightarrow$  (3) core-collapse (iron-core collapse) supernova explosion with NS (neon burning shell propagates to the center)

**Fate of the star is sensitive to its mass and nuclear e-capture and  $\beta$ -decay rates; Cooling of O-Ne-Mg core by nuclear URCA processes determines (2) or (3).**

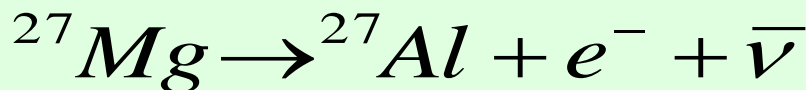
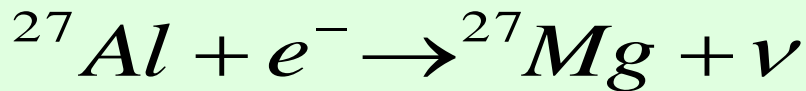
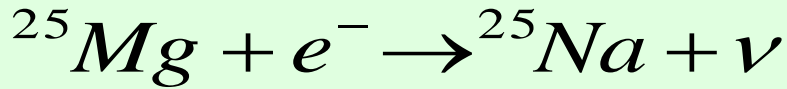
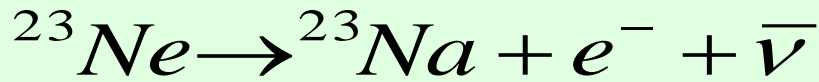
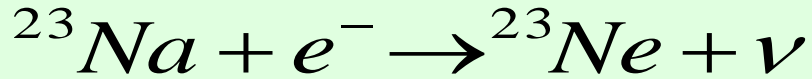
Nomoto and Hashimoto, Phys. Rep. 163, 13 (1988)

Miyaji, Nomoto, Yokoi, and Sugimoto, Pub. Astron. Soc. Jpn. 32, 303 (1980)

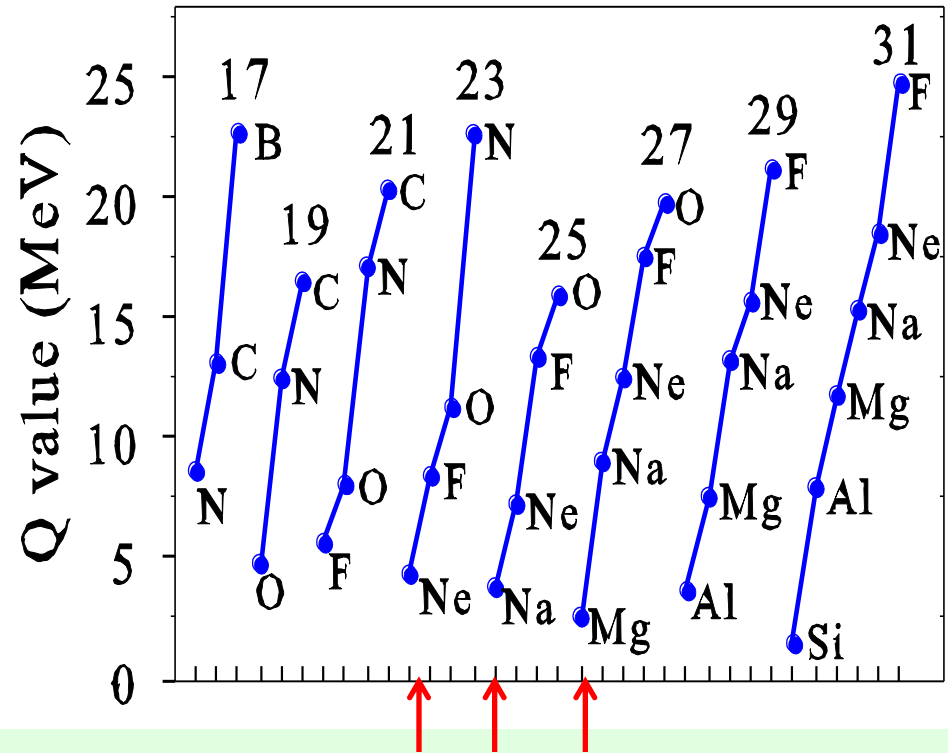
Nomoto, Astrophys. J. 277, 791 (1984); *ibid.* 322, 206 (1987)

# ▪ Detailed e-capture and beta-decay rates for URCA nuclear pairs in 8-10 solar-mass stars

Nuclear URCA process



Odd-A sd-shell Nuclei (A=17-31)



Cooling of O-Ne-Mg core of stars

→ ‘e-cap.SNe’ or ‘core-collapse SNe’

sd-shell: USDB Brown and Richter, PR C74, 034315 (2006)

Richter, Mkhize, Brown, PR C78, 064302 (2008)

# $(^{23}\text{Ne}, ^{23}\text{Na})$

PHYSICAL REVIEW C 88, 015806 (2013)

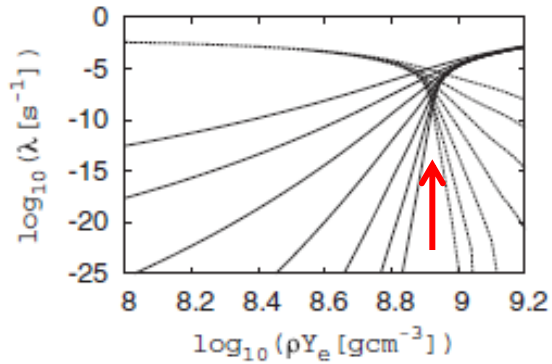


FIG. 2.  $\beta$ -transition rates for the  $A = 23$  URCA nuclear pair ( $^{23}\text{Ne}$ ,  $^{23}\text{Na}$ ) for various temperatures as functions of density  $\log_{10} \rho Y_e$ .  $\beta$ -decay rates (dashed lines) are those decreasing with density, while electron-capture rates (solid lines) are those increasing with density. The temperature steps are shown in the range of  $\log_{10} T = 8$  to  $9.2$  in steps of  $0.2$ .

$$\Delta \log_{10}(\rho Y_e) = 0.06$$

$$\Delta \log_{10}(\rho Y_e) = 0.2$$

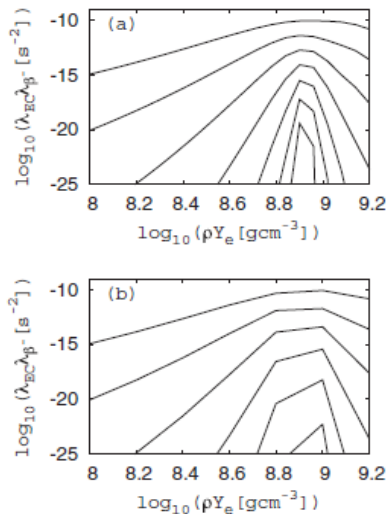


FIG. 3. Product of  $\beta$ -transition rates for the  $A = 23$  URCA nuclear pair ( $^{23}\text{Ne}$ ,  $^{23}\text{Na}$ ) for various temperatures as functions of density  $\log_{10} \rho Y_e$ . In panel (a), the mesh points are taken from  $\log_{10} \rho Y_e = 8.0$  to  $9.2$  in steps of  $0.02$ , while in panel (b), they are from  $\log_{10} \rho Y_e = 8.0$  to  $9.0$  in a single step as in Oda *et al.* [10].

$$8.0 < \log_{10}(\rho Y_e) < 9.2 \quad \text{in steps of } 0.02$$

$$8.0 < \log_{10} T < 9.2 \quad \text{in steps of } 0.05$$

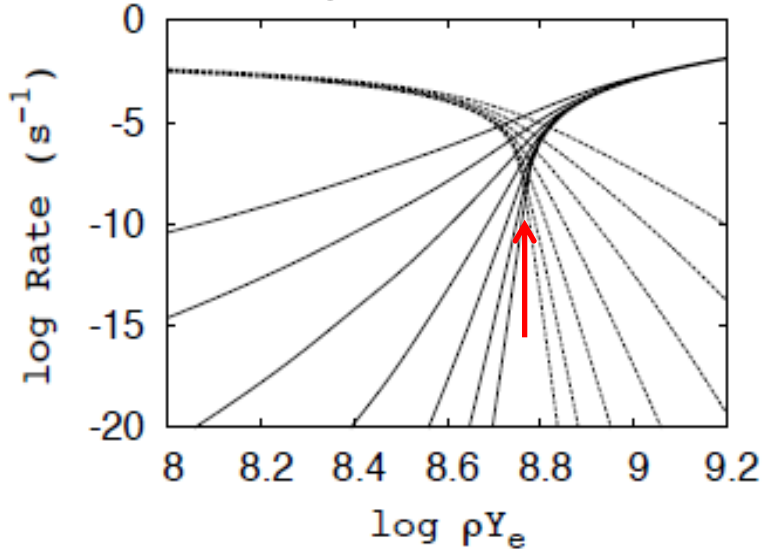
cf: Oda et al., At. Data and Nucl. Data Tables 56, 231 (1994):  $\Delta \log_{10}(\rho Y_e) = 1.0$

**URCA density at  $\log_{10} \rho Y_e = 8.92$  for  $A = 23$**



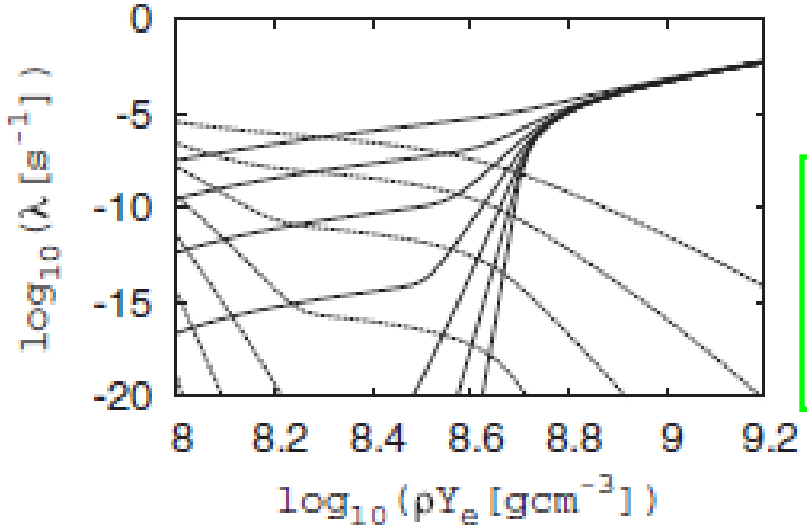
# Cooling of O-Ne-Mg core by the nuclear URCA processes

(<sup>25</sup>Na, <sup>25</sup>Mg)

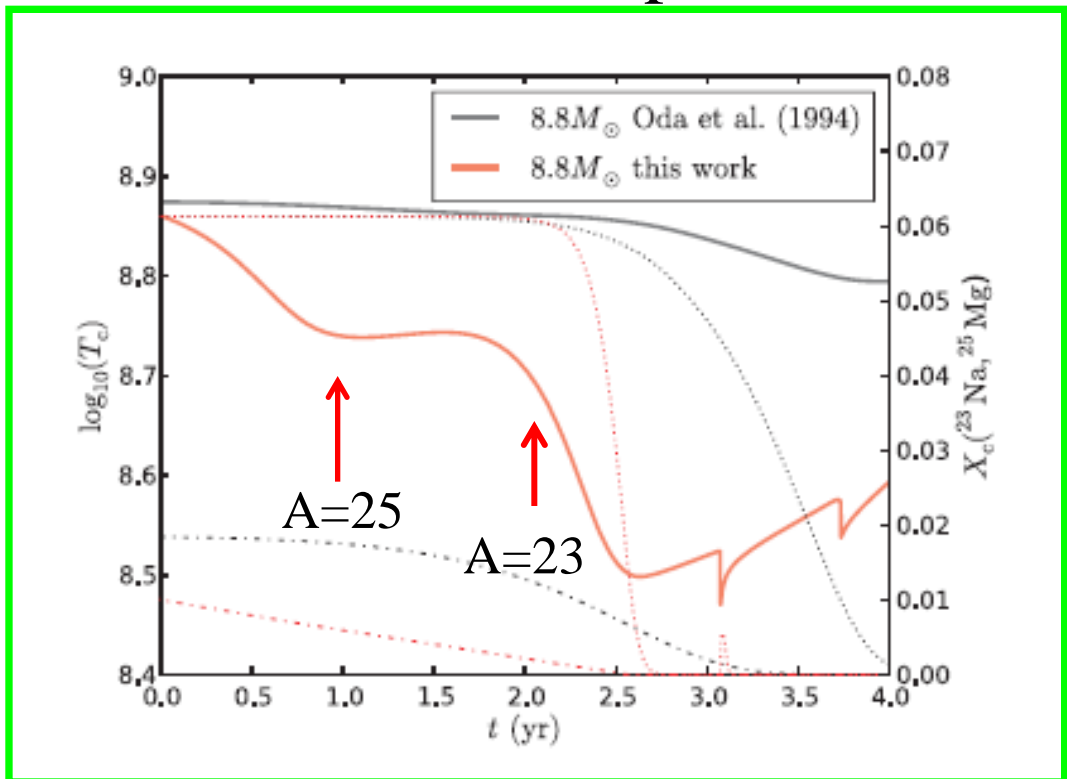


URCA density at  $\log_{10} \rho Y_e = 8.78$

(<sup>27</sup>Mg, <sup>27</sup>Al) g.s. 1/2<sup>+</sup> & 5/2<sup>+</sup>



No clear URCA density for A=27



8.8M<sub>⊙</sub> star collapses triggered by subsequent e-capture on <sup>24</sup>Mg and <sup>20</sup>Ne (e-capture supernova explosion)

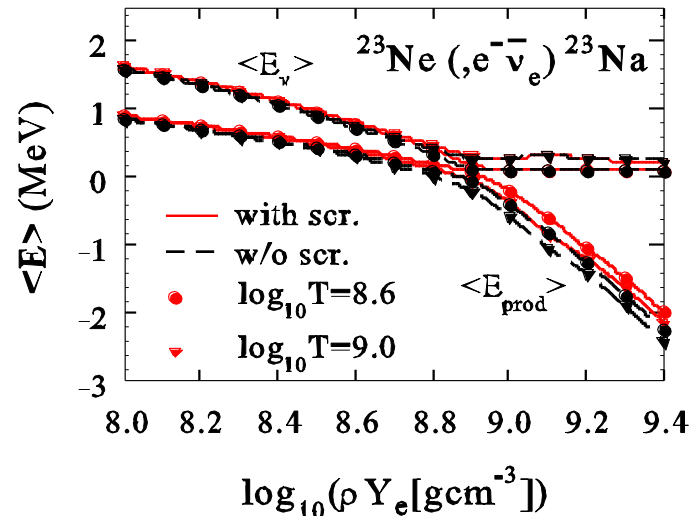
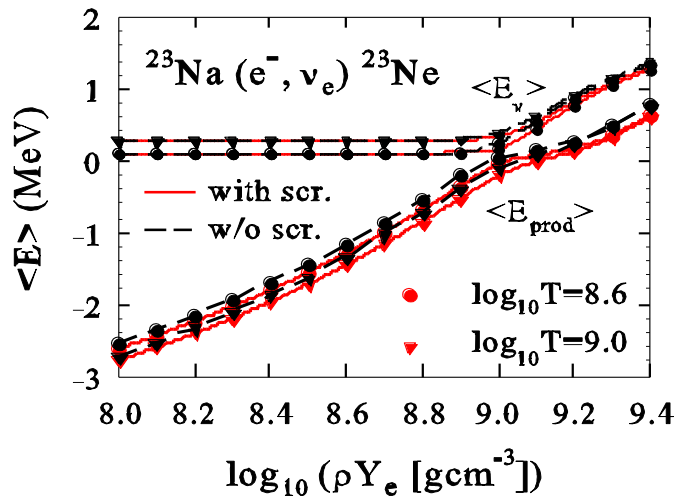
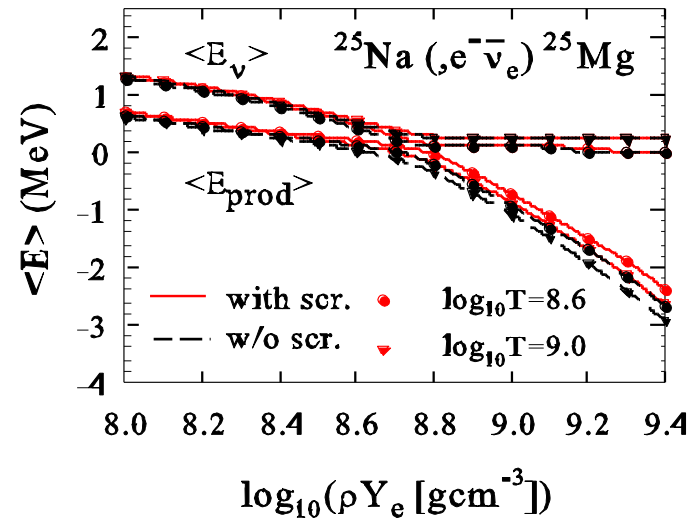
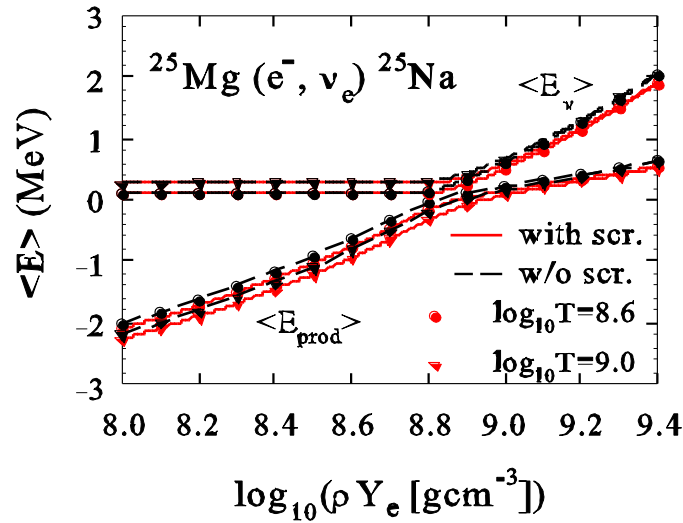
Toki, Suzuki, Nomoto, Jones and Hirschi, PR C 88, 015806 (2013)  
 Jones et al., Astrophys. J. 772, 150 (2013)

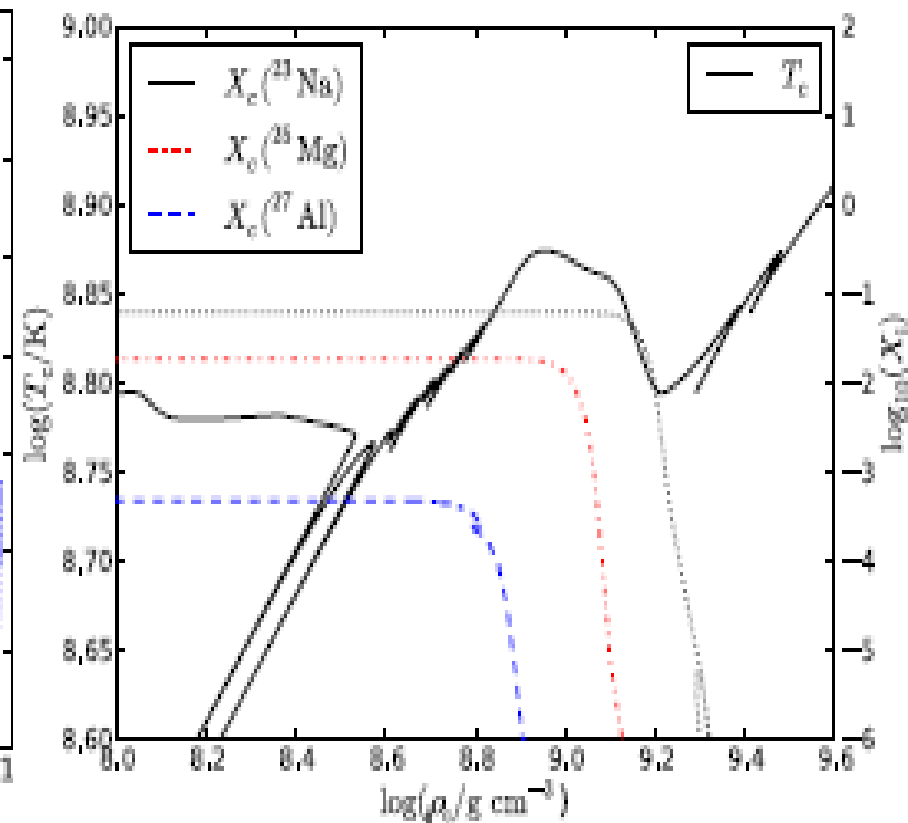
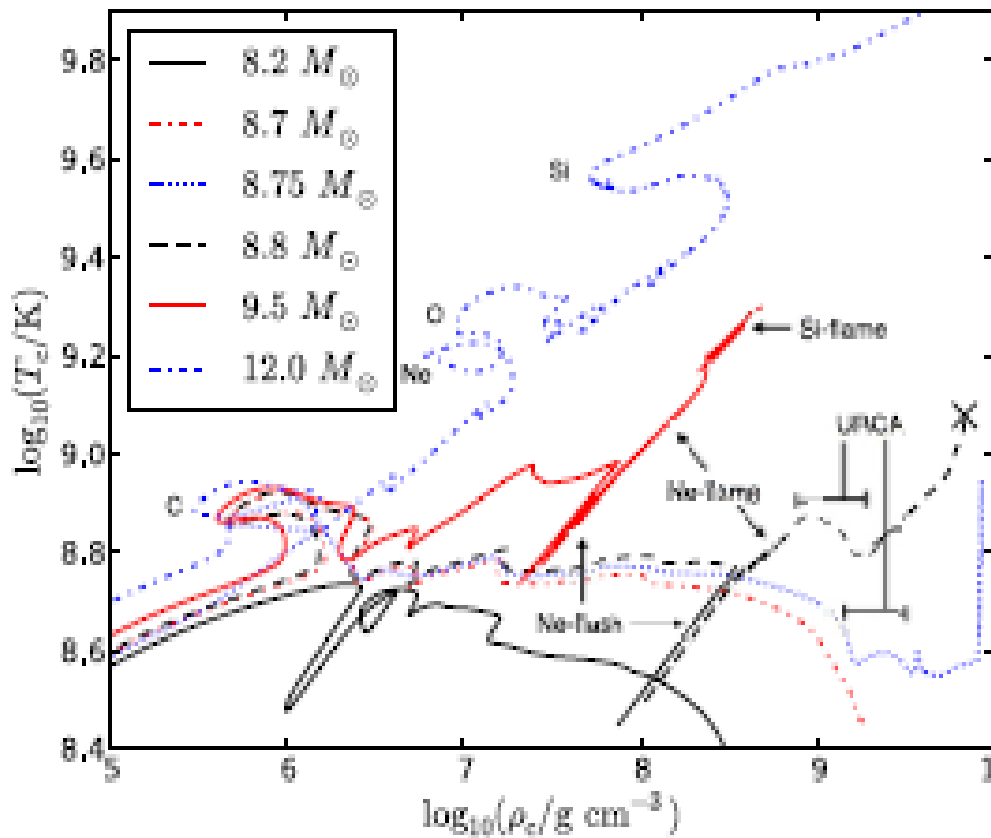
# Energy generation and $\nu$ cooling

$$\langle E_{\text{prod}} \rangle = \mu_e - Q_{\text{nucl}} - \langle E_\nu \rangle \quad kT \frac{ds}{dt} = \frac{dY_e}{dt} \langle E_{\text{prod}} \rangle$$

$$Q_{\text{nucl}} = M_d c^2 - M_p c^2,$$

$$\langle E_{\text{prod}} \rangle = Q_{\text{nucl}} - \mu_e - \langle E_\nu \rangle$$





Summary of Model Properties

	$8.2 M_{\odot}$	$8.7 M_{\odot}$	$8.75 M_{\odot}$	$8.8 M_{\odot}$	$9.5 M_{\odot}$	$12.0 M_{\odot}$
Remnant	ONe WD	ONe WD/NS	NS	NS	NS	NS
SN type	...	.../EC-SN (IIP)	EC-SN (IIP)	EC-SN (IIP)	CC-SN (IIP)	CC-SN (IIP)

# Coulomb corrections: screening effects

## 1. Screening effects of electrons

$V(r)$  with screening effects of relativistic degenerate electron liquid

$$V_s(r) = V(r) - \left( -\frac{Ze^2}{r} \right) = Ze^2(2k_F)J,$$

$$\begin{aligned} V(r) &= -\frac{Ze^2}{2\pi^2} \int \frac{e^{i\vec{k}\vec{r}}}{k^2\epsilon(k, 0)} d^3k \\ &= -\frac{Ze^2 2k_F}{2k_F r} \frac{2}{\pi} \int \frac{\sin(2k_F qr)}{q^2\epsilon(q, 0)} dq. \end{aligned}$$

Juodagalvis et al., Nucl. Phys. A 848, 454 (2010).

Itoh et al, Astrophys. J. 579, 380 (2002).

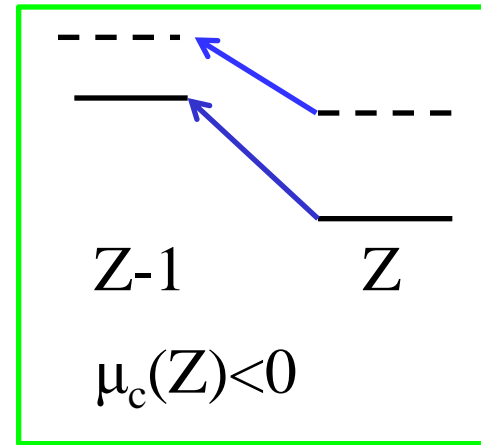
$V_s(0) > 0 \rightarrow$  **reduce (enhance) e-capture ( $\beta$ -decay) rates**

## 2. Change of threshold energy

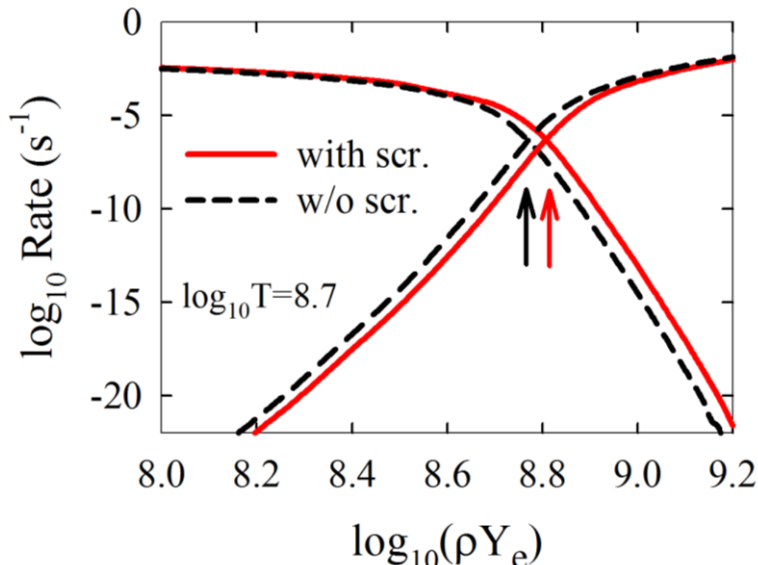
$$\Delta Q_c = \mu_c(Z-1) - \mu_c(Z),$$

$\mu_c(Z)$  = the correction of the chemical potential of the ion with  $Z$

$\Delta Q_c \rightarrow$  **reduce e-capture rates & enhance  $\beta$ -decay rates**



$^{25}\text{Na} \leftrightarrow ^{25}\text{Mg}$



Slattery, Doolen, DeWitt, Phys. Rev. A26, 2255 (1982).

Ichimaru, Rev. Mod. Phys. 65, 255 (1993).

$$\rho Y_e = 8.78 \rightarrow 8.81$$

**URCA density  $\rightarrow$  higher density region**



# Strong neutrino cooling by cycles of electron capture and $\beta^-$ decay in neutron star crusts

H. Schatz<sup>1,2,3</sup>, S. Gupta<sup>4</sup>, P. Möller<sup>2,5</sup>, M. Beard<sup>2,6</sup>, E. F. Brown<sup>1,2,3</sup>, A. T. Deibel<sup>2,3</sup>, L. R. Gasques<sup>7</sup>, W. R. Hix<sup>8,9</sup>, L. Keek<sup>1,2,3</sup>, R. Lau<sup>1,2,3</sup>, A. W. Steiner<sup>2,10</sup> & M. Wiescher<sup>2,6</sup>

**Table 1 | Electron-capture/ $\beta^-$ -decay pairs with highest cooling rates**

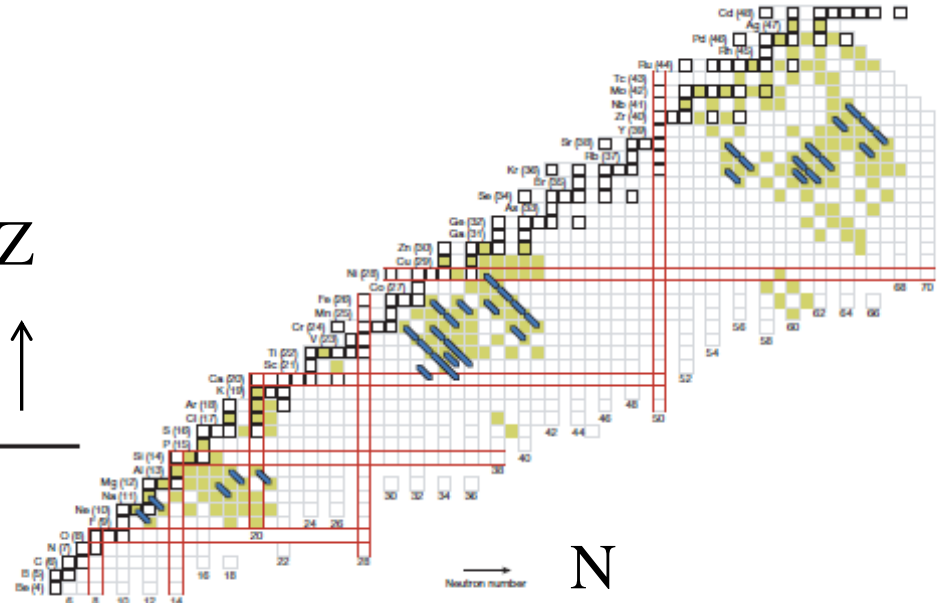
Electron-capture/ $\beta^-$ -decay pair		Density <sup>†</sup>	Chemical potential <sup>†</sup>	Luminosity <sup>‡</sup>
Parent	Daughter*	( $10^{10} \text{ g cm}^{-3}$ )	(MeV)	( $10^{36} \text{ erg s}^{-1}$ )
<sup>29</sup> Mg	<sup>29</sup> Na	4.79	13.3	24
<sup>55</sup> Ti	<sup>55</sup> Sc, <sup>55</sup> Ca	3.73	12.1	11
<sup>31</sup> Al	<sup>31</sup> Mg	3.39	11.8	8.8
<sup>33</sup> Al	<sup>33</sup> Mg	5.19	13.4	8.3
<sup>56</sup> Ti	<sup>56</sup> Sc	5.57	13.8	3.5
<sup>57</sup> Cr	<sup>57</sup> V	1.22	8.3	1.6
<sup>57</sup> V	<sup>57</sup> Ti, <sup>57</sup> Sc	2.56	10.7	1.6
<sup>63</sup> Cr	<sup>63</sup> V	6.82	14.7	0.97
<sup>105</sup> Zr	<sup>105</sup> Y	3.12	11.2	0.92
<sup>59</sup> Mn	<sup>59</sup> Cr	0.945	7.6	0.88
<sup>103</sup> Sr	<sup>103</sup> Rb	5.30	13.3	0.65
<sup>96</sup> Kr	<sup>96</sup> Br	6.40	14.3	0.65
<sup>65</sup> Fe	<sup>65</sup> Mn	2.34	10.3	0.60
<sup>65</sup> Mn	<sup>65</sup> Cr	3.55	11.7	0.46

Z



N

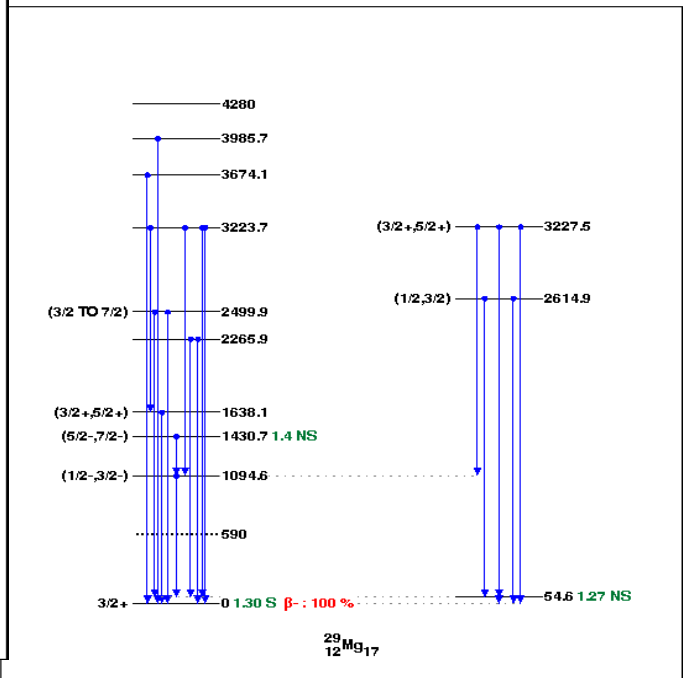
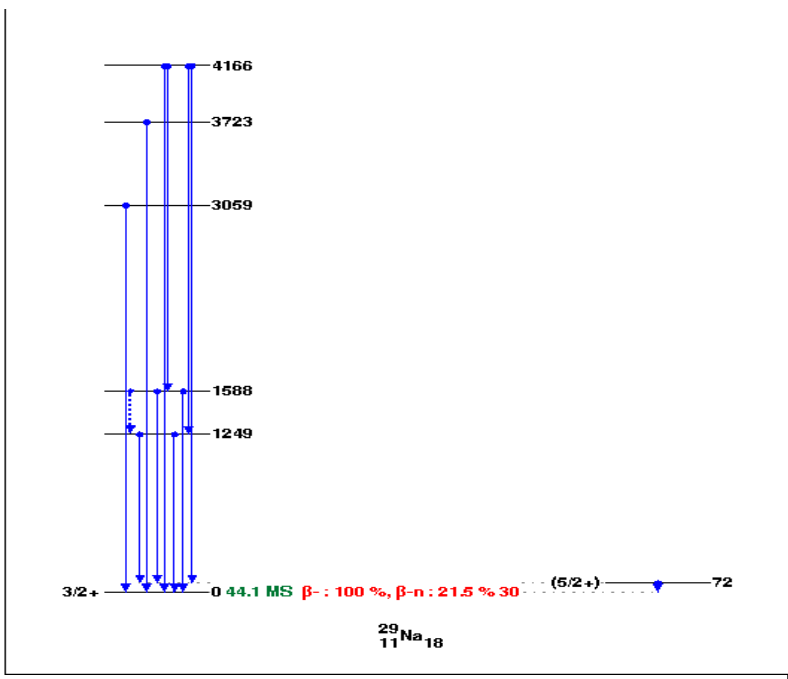
Neutron number



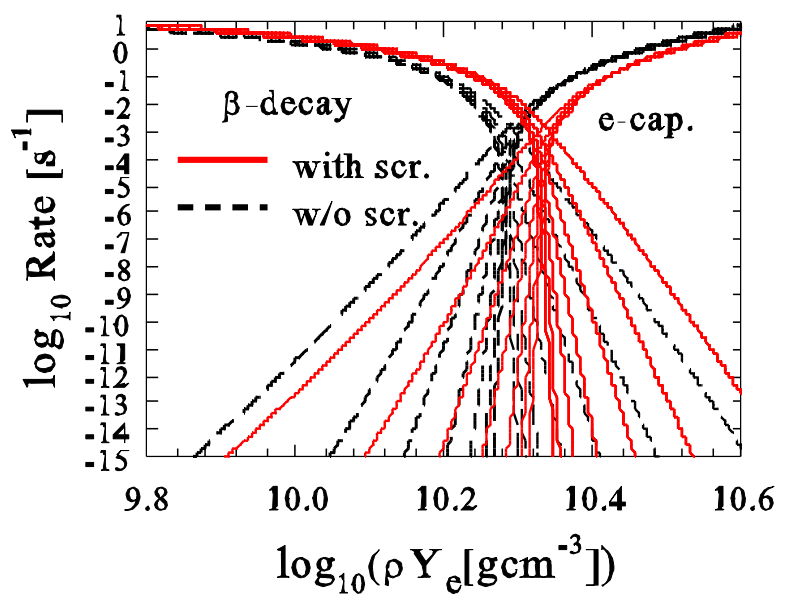
**Figure 2 | Electron-capture/ $\beta^-$ -decay pairs on a chart of the nuclides.** The thick blue lines denote electron-capture/ $\beta^-$ -decay pairs that would generate a strong neutrino luminosity in excess of  $5 \times 10^{34} \text{ erg s}^{-1}$  at  $T = 0.51 \text{ GK}$  for a composition consisting entirely of the respective electron-capture/ $\beta^-$ -decay pair. They largely coincide with regions where allowed electron-capture and  $\beta^-$ -decay transitions are predicted to populate low-lying states and subsequent electron capture is blocked (shaded squares, see also the discussion

in ref. 3). These are mostly regions between the dashed neutron and proton shells (pairs of horizontal and vertical red lines), where nuclei are significantly deformed (see Supplementary Information section 4). Nuclides that are  $\beta^-$ -stable under terrestrial conditions are shown as squares bordered by thicker lines. Nuclear charge numbers are indicated in parentheses next to element symbols.

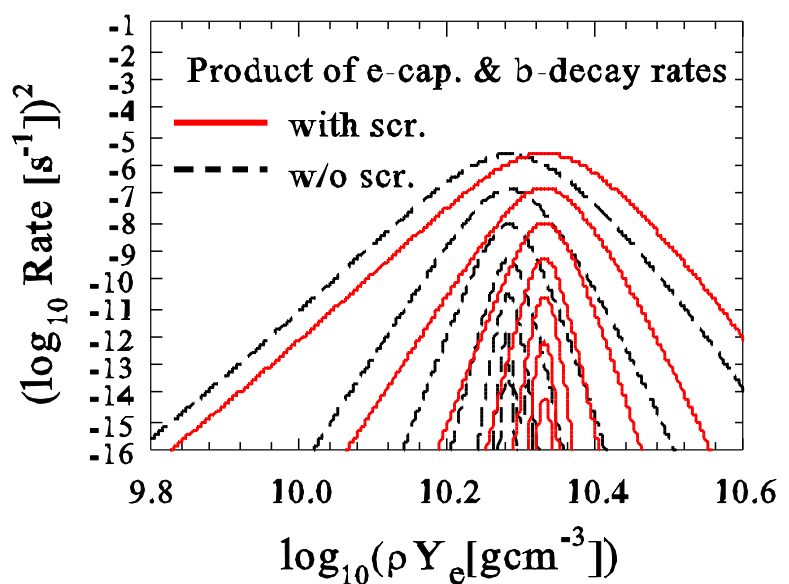
20Cel

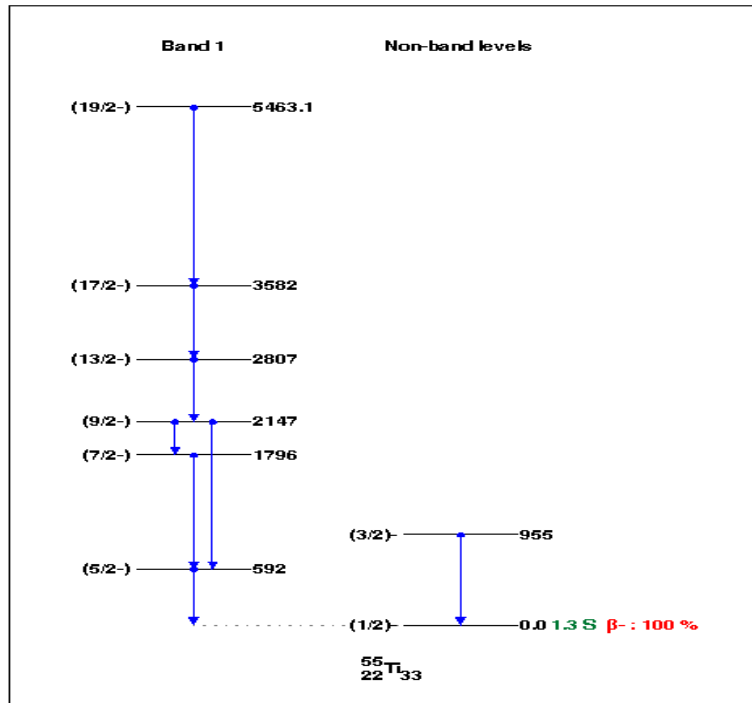
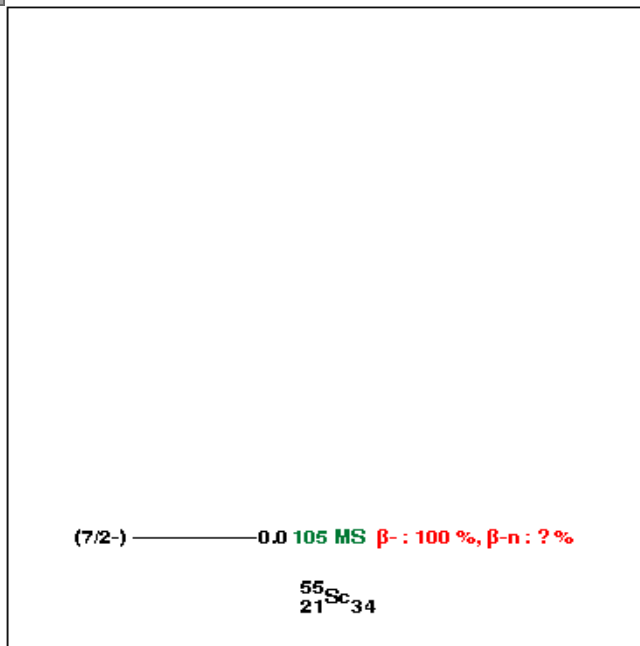


$^{29}\text{Mg} \leftrightarrow ^{29}\text{Na}$

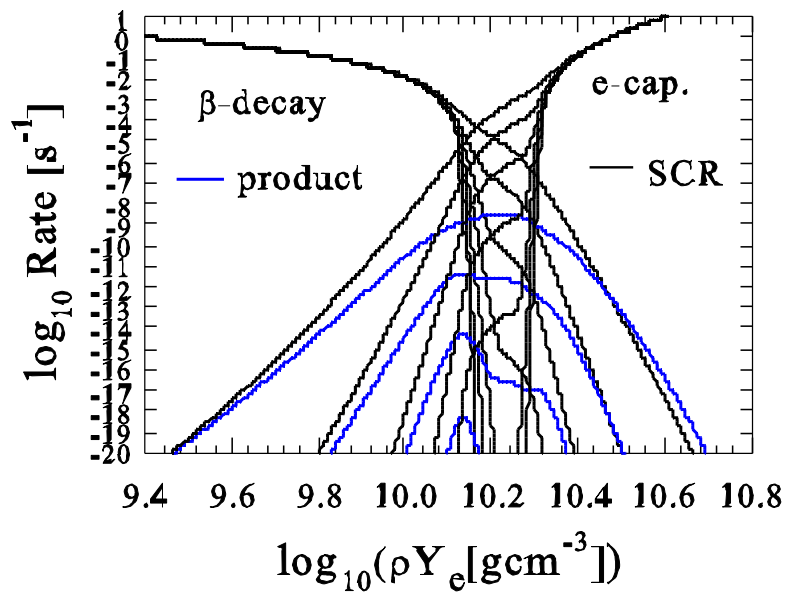


$^{29}\text{Mg} \leftrightarrow ^{29}\text{Na}$

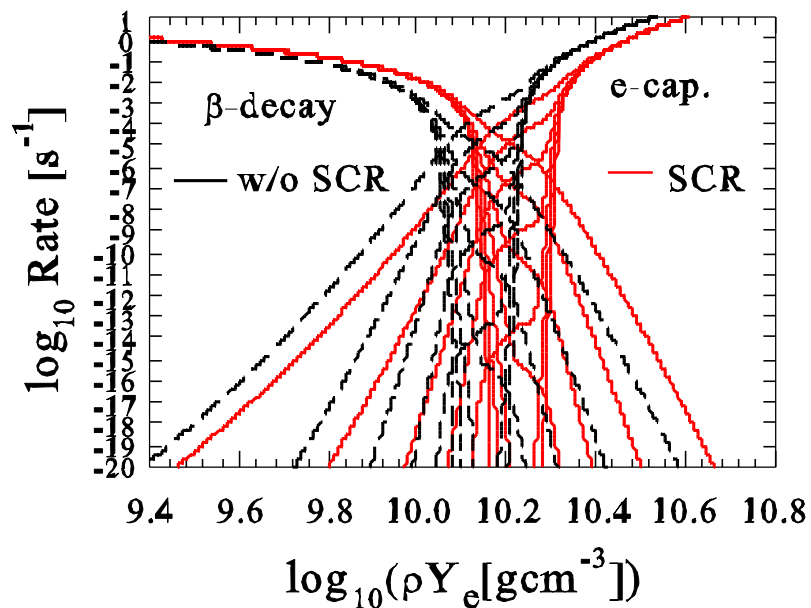




$^{55}\text{Ti} (1/2^-) \leftrightarrow ^{55}\text{Sc} (7/2^-)$



$^{55}\text{Ti} (1/2^-) \leftrightarrow ^{55}\text{Sc} (7/2^-)$



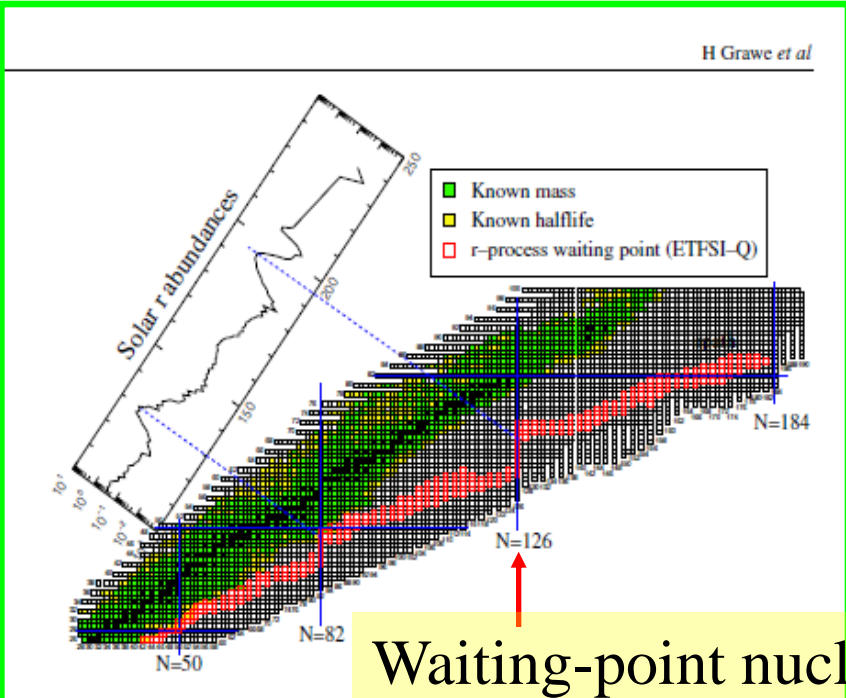


# ○ Beta-Decays of r-process waiting-point nuclei at N=126

R-process

Shell Model

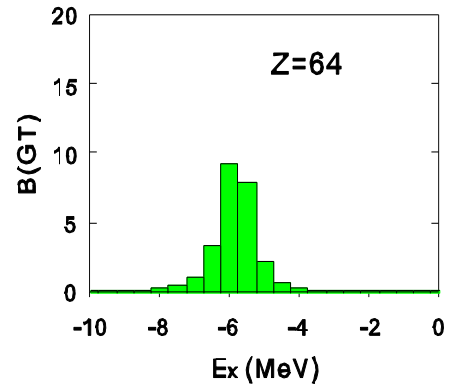
Z=64-73



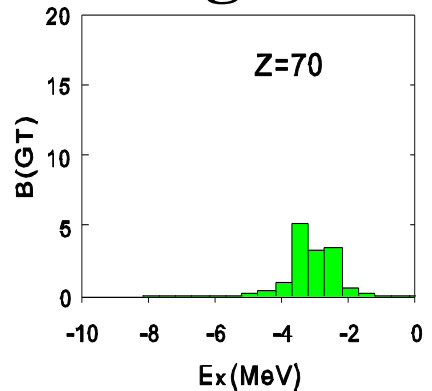
Waiting-point nuclei

Figure 18. The figure shows the range of r-process paths, defined by their waiting point nuclei. After decay to stability the abundance of the r-process progenitors produce the observed solar r-process abundance distribution. The r-process paths run generally through neutron-rich nuclei with experimentally unknown masses and half lives. In this calculation a mass formula based on the ETFSI model and special treatment of shell quenching [79] has been adopted (courtesy of Kratz and Schatz).

## Gamow-Teller strengths

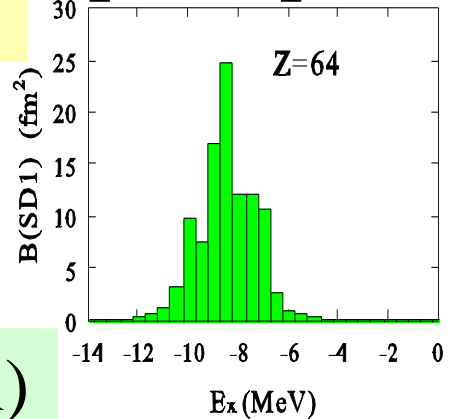


$\sum B(GT) = 14.4$

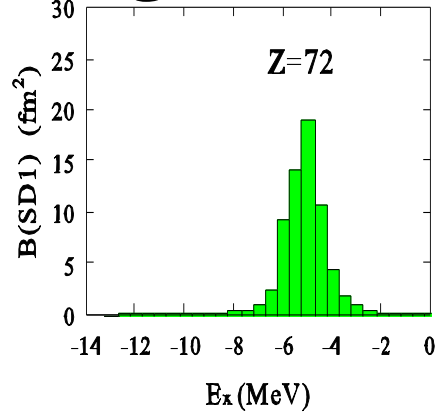


$\sum B(GT) = 8.5$

## Spin-dipole strengths: 1-



$\sum SD1 = 55.5 \text{ fm}^2$



$\sum SD1 = 40.1 \text{ fm}^2$

Beta-decay: GT + FF (first-forbidden)

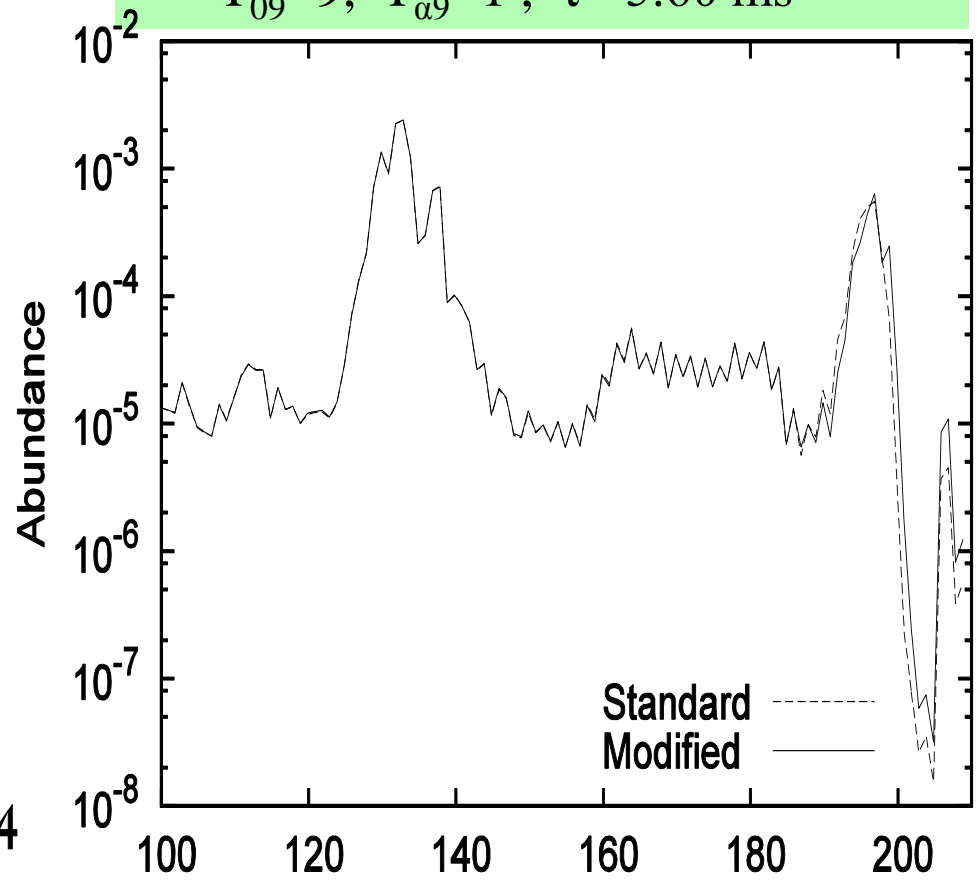
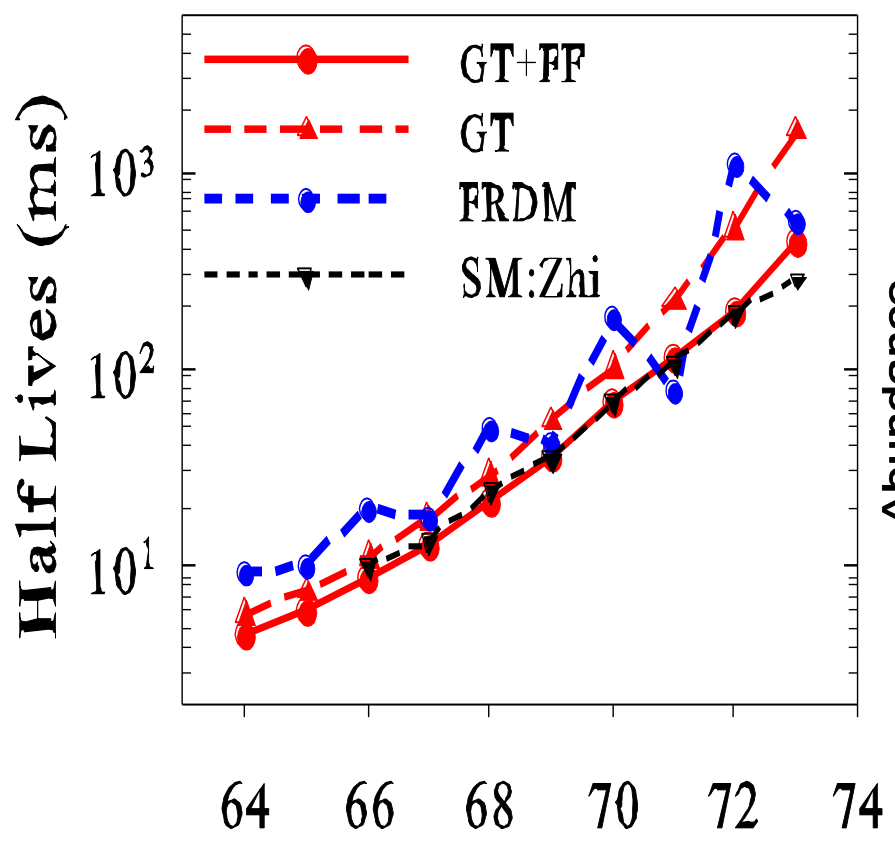
# Half-lives of N=126 isotones GT + FF (first-forbidden)

# r-process nucleosynthesis

Constant Entropy Wind Model

$$T_9 = (T_{09} - T_{\alpha 9}) \exp(-t/\tau) + T_{\alpha 9}$$

$$T_{09} = 9, \quad T_{\alpha 9} = 1, \quad \tau = 5.60 \text{ ms}$$

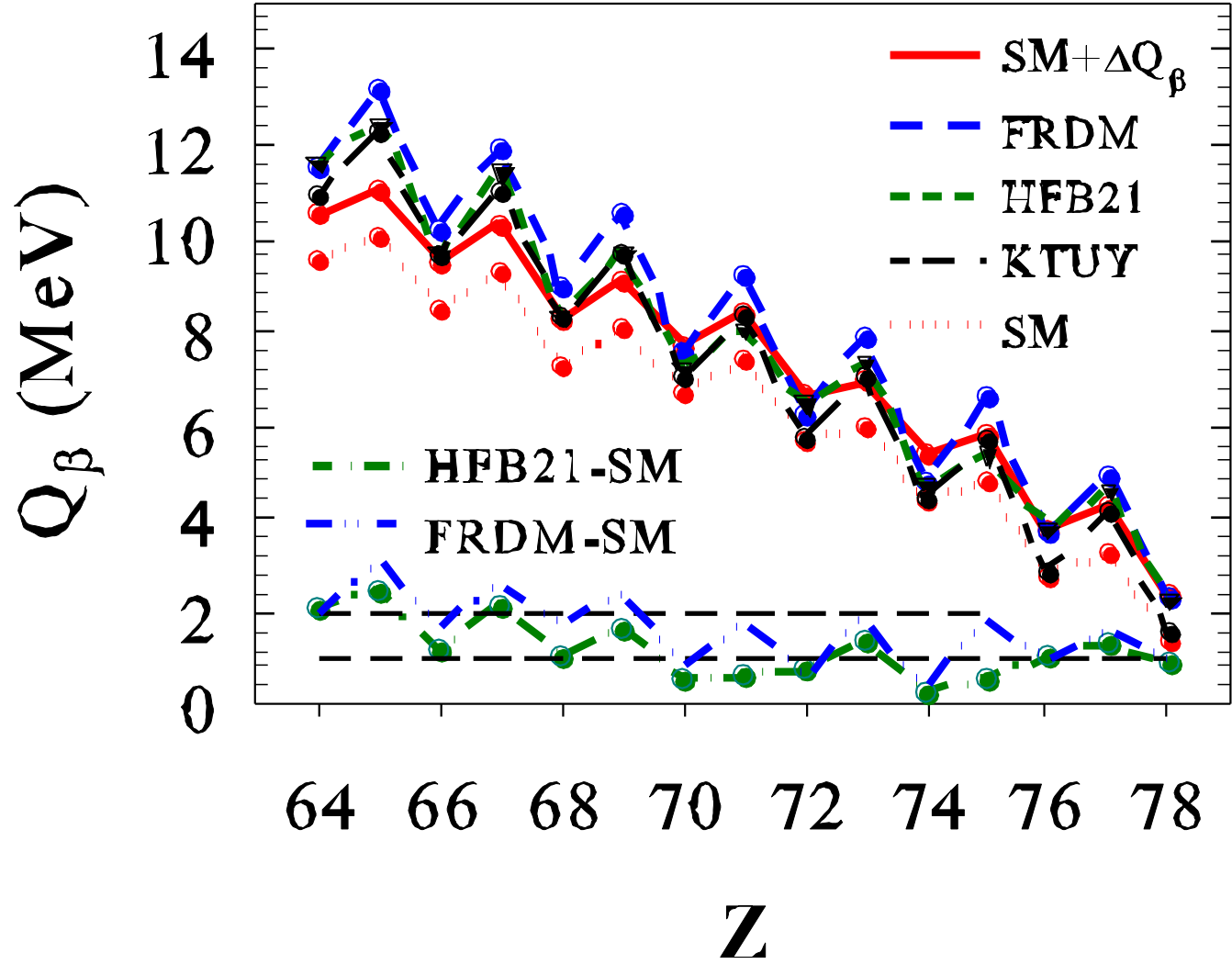


$$Q = g_A^{\text{eff}} / g_A = 0.7 \quad Z$$

Suzuki, Yoshida, Kajino, Otsuka,  
PR C85, 014802 (2012)

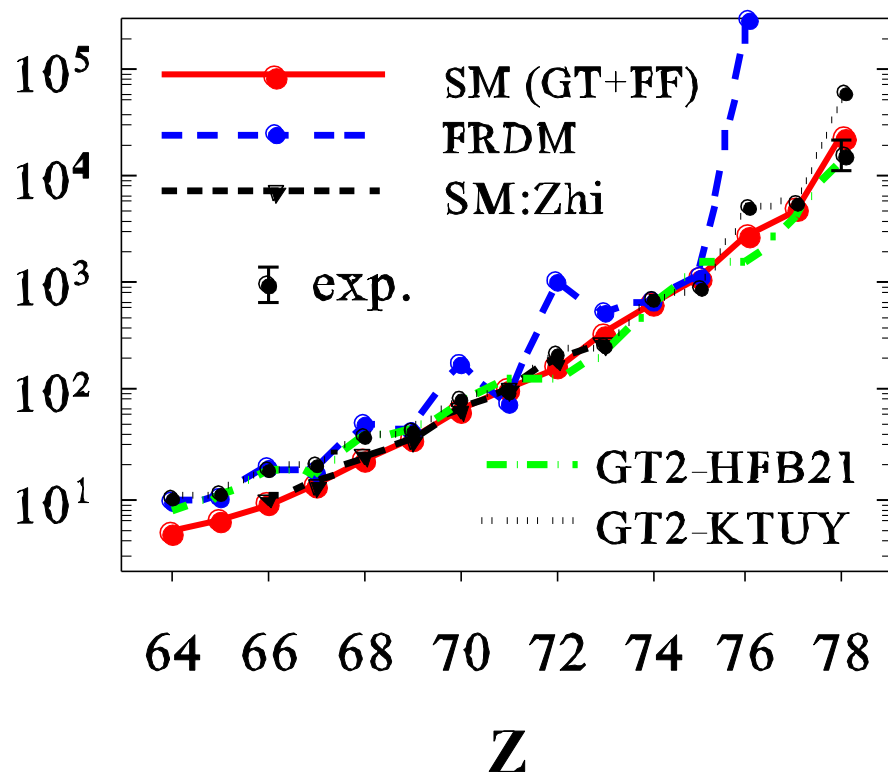
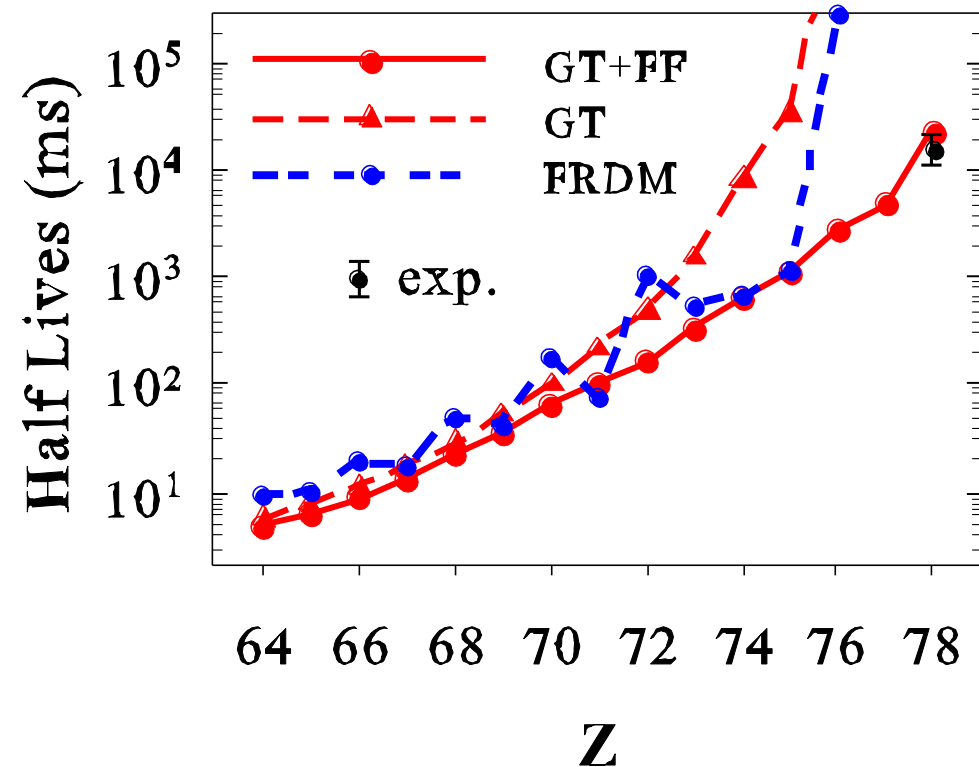
Mass Number A

Half-lives:  
 - - - Standard (Moller et al.)  
 — Modified



$\Delta Q = 1$  MeV

# r-process nucleosynthesis up to Th and U



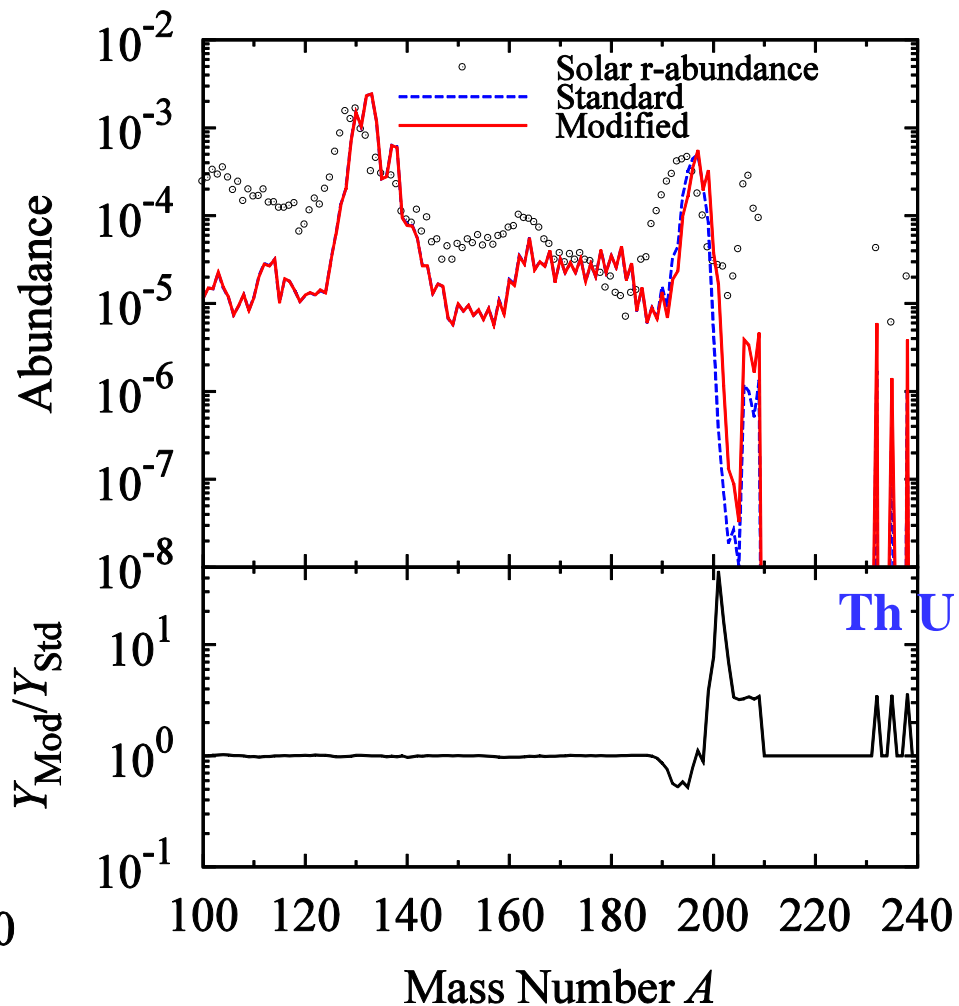
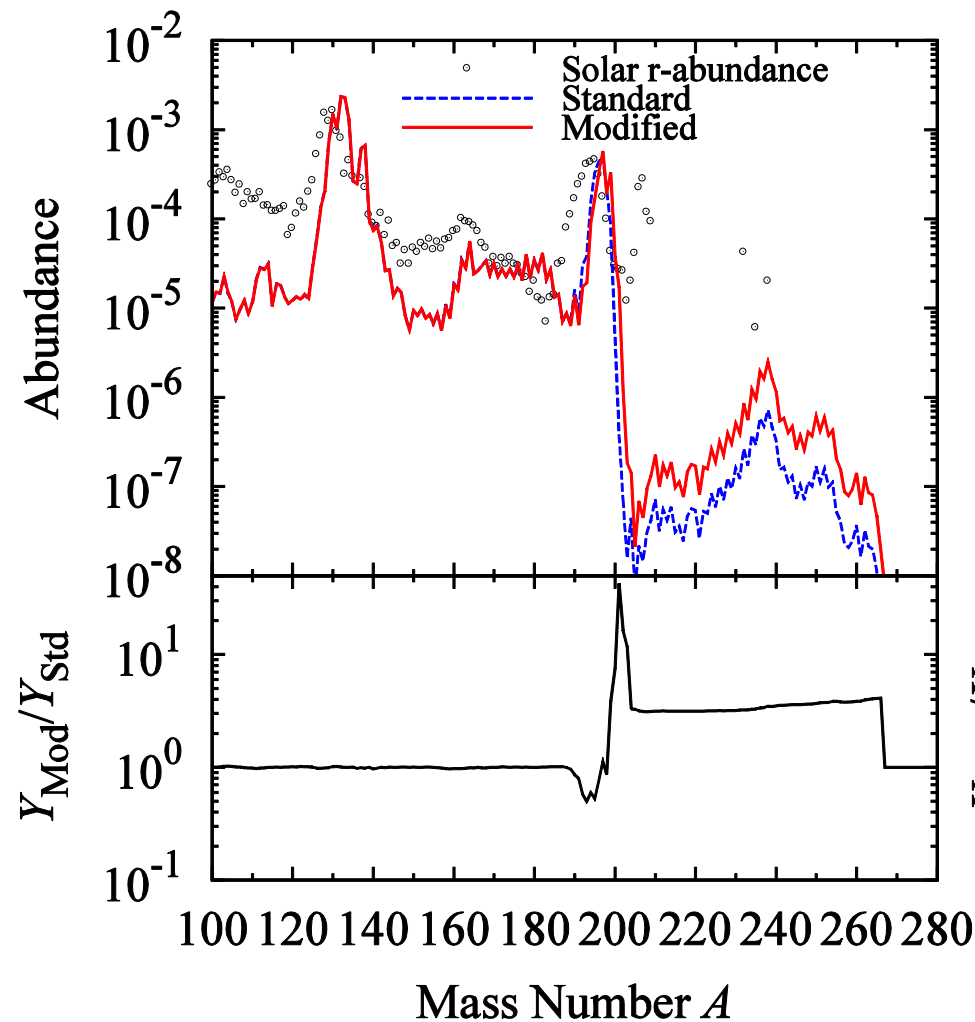
GT:  $q(g_A)=0.7$

FF:  $q(g_A)=0.34$ ,  $q(g_V)=0.67$

Z=78:  $^{204}\text{Pt}$   $t_{1/2}(\text{exp}) = 16 +6/-5 \text{ s}$  Morales et al., PRL 113 (2014)

Before beta-decays

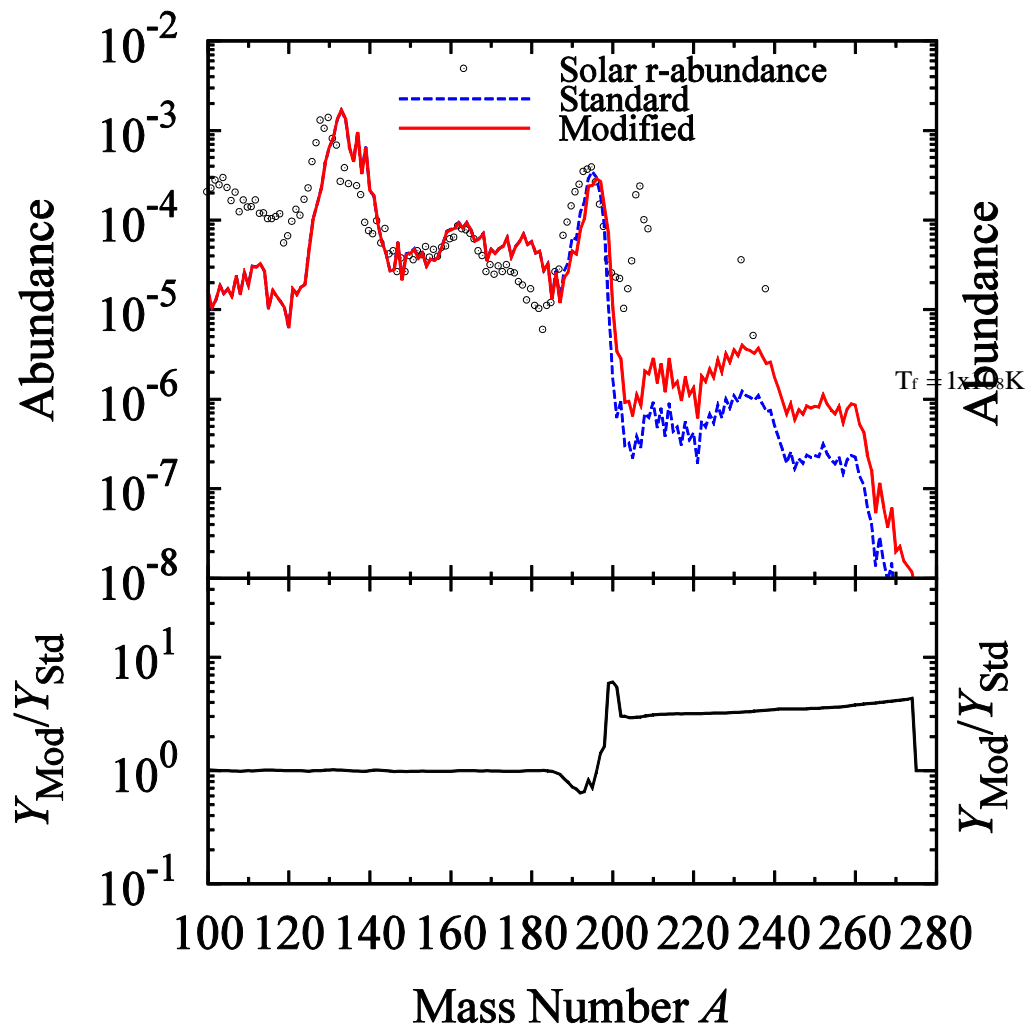
After beta-decays



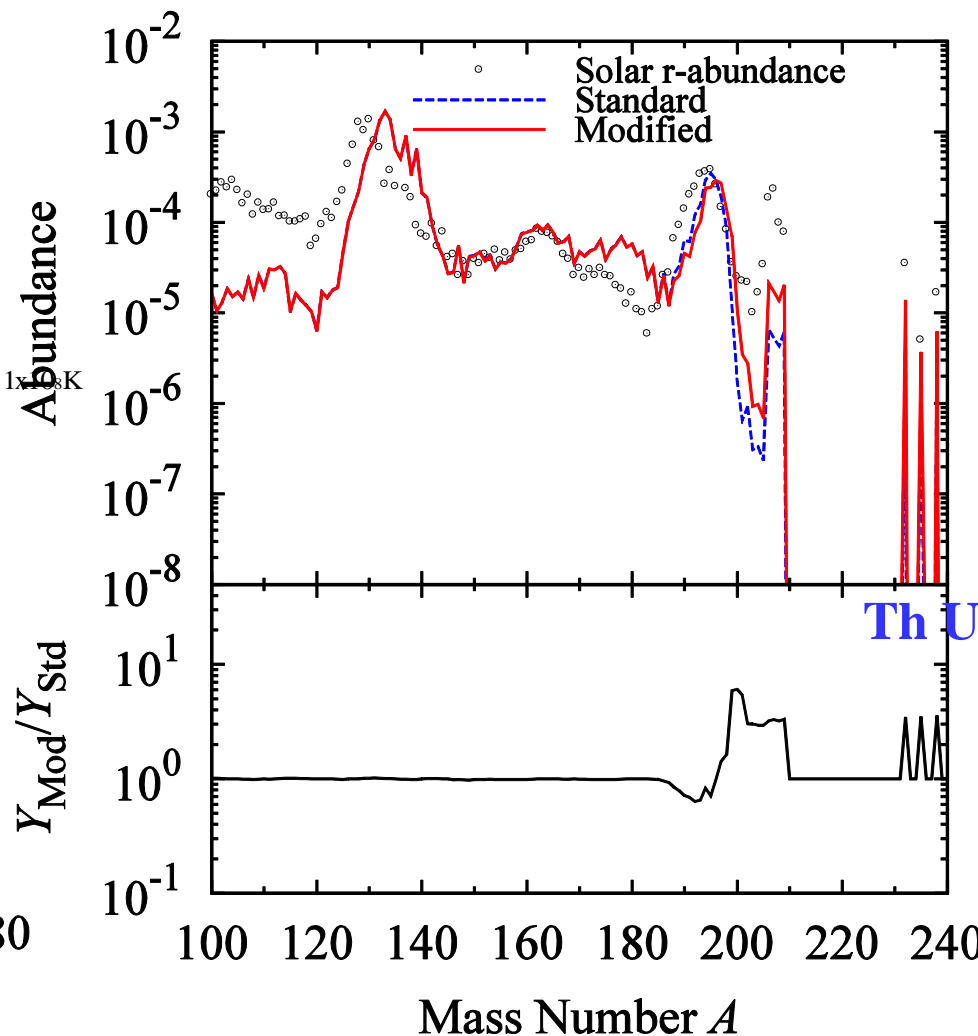
Standard = FRDM

Cold case:  $T_f = 1 \times 10^8$  K

Before beta-decays

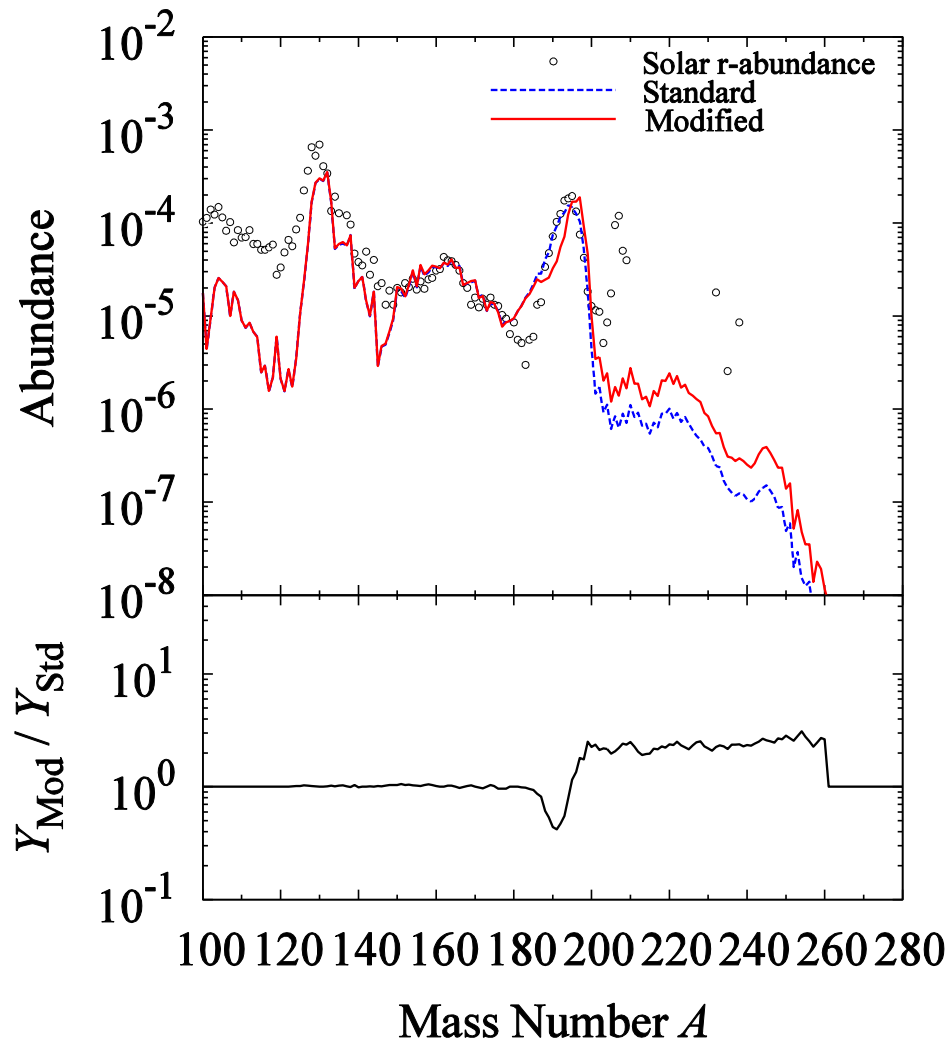


After beta-decays



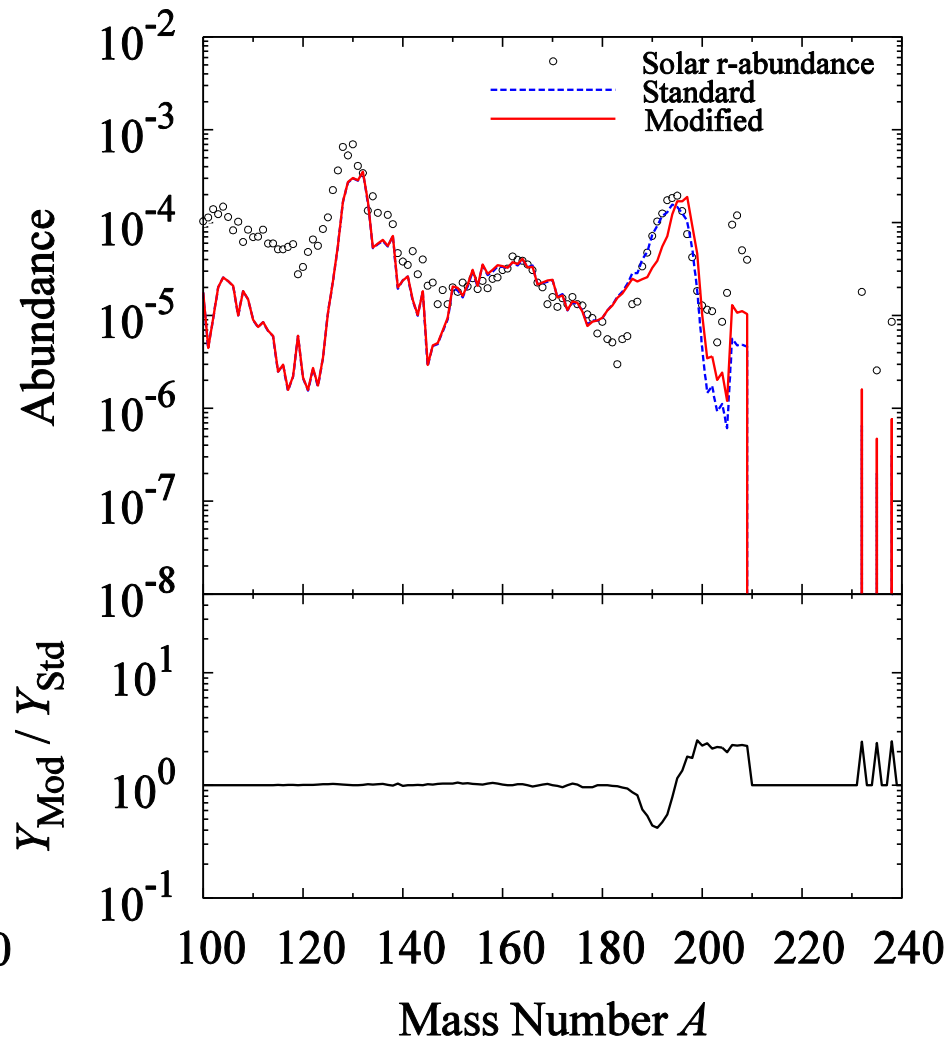
# MHD-jet SNe

## Before beta-decays



# Shibagaki-Kajino

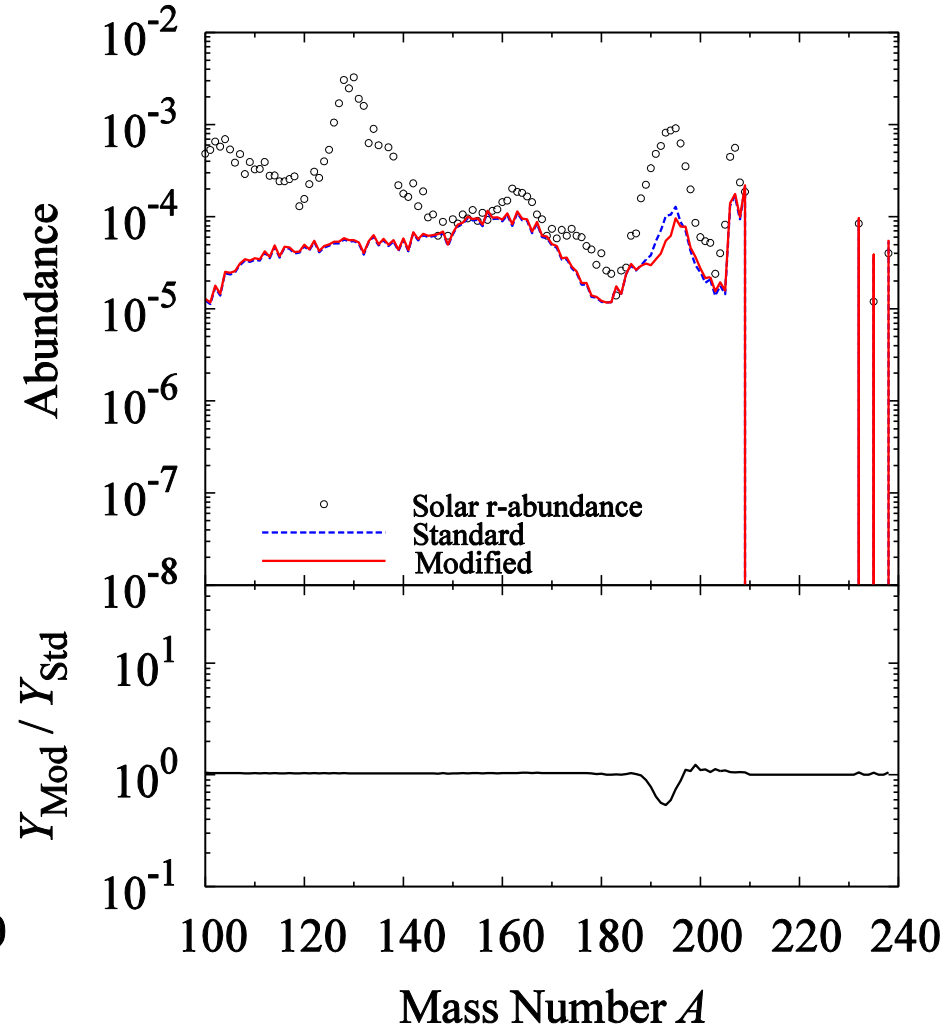
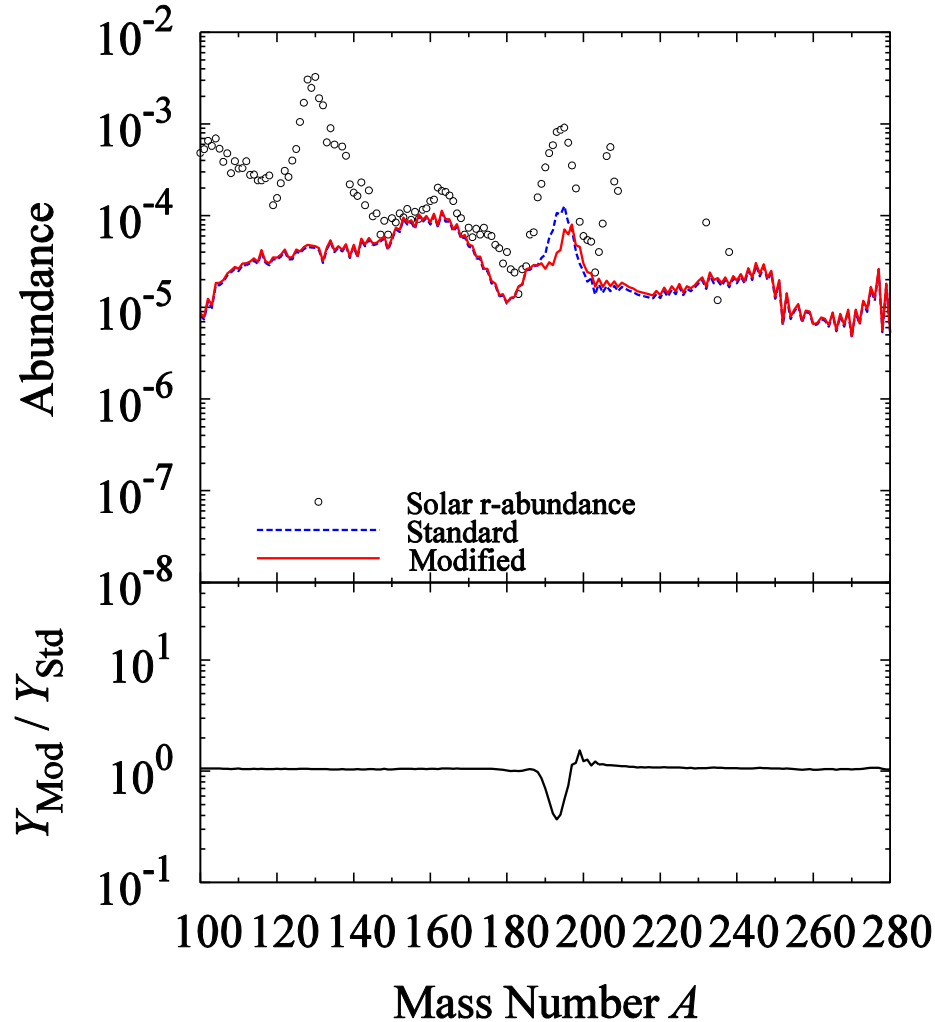
## After beta-decays



Standard = GT2-KTUY

# r-process nucleosynthesis in neutron-star mergers

Shibagaki & Kajino

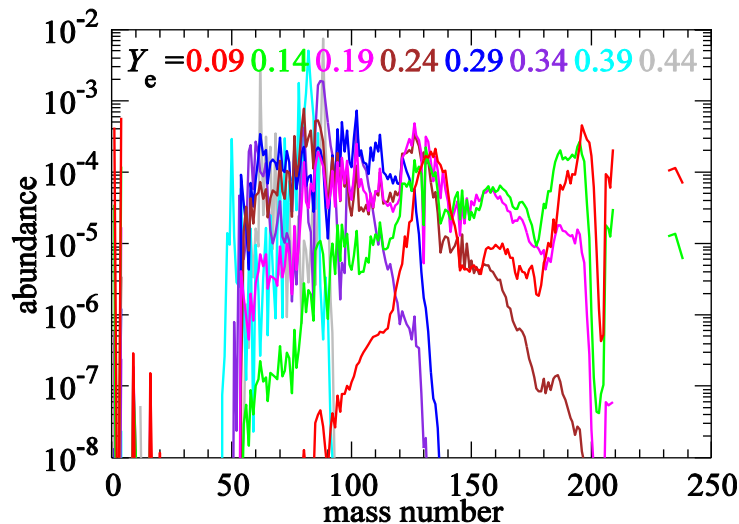


Standard = GT2-KTUY



# r-process nucleosynthesis in neutron-star mergers

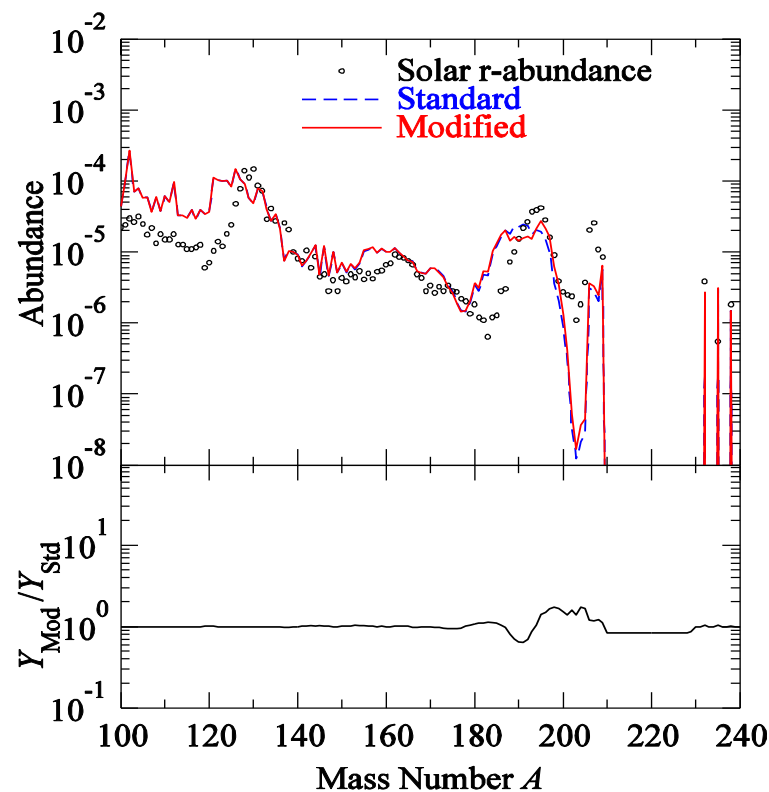
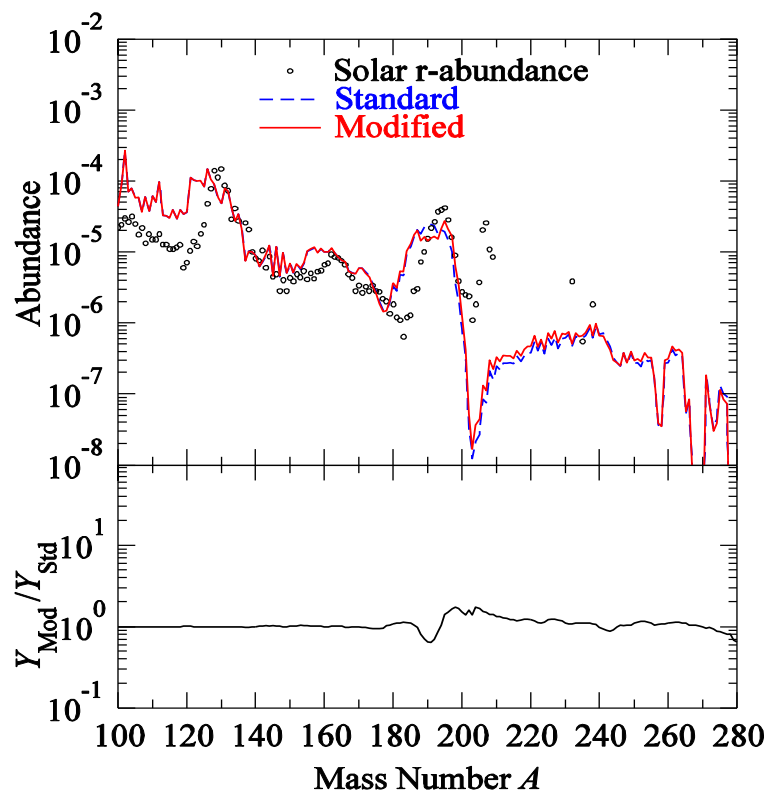
Wanajo



$$Y_e = 0.09 - 0.44$$

Standard: GT2-HFB21

Modified: SM at N=126



# Summary

- **New  $\nu$  –induced cross sections based on new shell-model Hamiltonians (SFO for p-shell, GXPF1 for pf-shell)**
- **Good reproduction of experimental data for  $^{12}\text{C}(\nu, e^-)^{12}\text{N}$ ,  $^{12}\text{C}(\nu, \nu')^{12}\text{C}$  and  $^{56}\text{Fe}(\nu, e^-)^{56}\text{Co}$**
- **Effects of  $\nu$ -oscillations in nucleosynthesis abundance ratio of  $^7\text{Li}/^{11}\text{B} \rightarrow \nu$  mass hierarchy**
- **GXPF1J well describes the GT strengths in Ni isotopes :  $^{56}\text{Ni}$  two-peak structure confirmed by recent exp.**
  - ▪ **Accurate evaluation of e-capture rates at stellar environments**  
**Nucleosynthesis in Type-I SNe;  $^{58}\text{Ni}/^{56}\text{Ni}$  reduced**
  - ▪ **Enhancement of  $^{56}\text{Ni}(\nu, \nu'p)^{55}\text{Co}$  reaction cross sections and production yield of  $^{55}\text{Mn}$  in Pop III stars**

- **Detailed e-capture and beta-decay rates for URCA nuclear pairs in 8-10 solar-mass stars**
  - **URCA density for  $A=25$  and  $23$  with fine mesh of density and temperature**
  - **Cooling of O-Ne-Mg core by nuclear URCA processes determines the fate of the stars.**
- **URCA processes in neutron star crusts**
  - $^{29}\text{Mg}$ - $^{29}\text{Na}$ ,  $^{55}\text{Ti}$ - $^{55}\text{Sc}$  pairs**
- **Half-lives of  $N=126$  isotones are evaluated by shell-model calculations with GT and FF contributions.**
  - **Shorter half-lives than FRDM**
  - r-process nucleosynthesis up to Th and U at SNe and neutron-star mergers**

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